

1 **iHDSel software: The Price equation and the population stability index**
2 **to detect genomic patterns compatible with selective sweeps. An**
3 **example with SARS-CoV-2.**

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10 **Abstract**

11 A large number of methods have been developed and continue to be developed for detecting the
12 signatures of selective sweeps in genomes. Significant advances have been made, including the
13 combination of different statistical strategies and the incorporation of artificial intelligence
14 (machine learning) methods. Despite these advances, several common problems persist, such as
15 the unknown null distribution of the statistics used, necessitating simulations and resampling to
16 assign significance to the statistics. Additionally, it is not always clear how deviations from the
17 specific assumptions of each method might affect the results.

18 In this work, allelic classes of haplotypes are used along with the informational interpretation of
19 the Price equation to design a statistic with a known distribution that can detect genomic patterns
20 caused by selective sweeps. The statistic consists of Jeffreys divergence, also known as the
21 population stability index, applied to the distribution of allelic classes of haplotypes in two
22 samples. Results with simulated data show optimal performance of the statistic in detecting
23 divergent selection. Analysis of real SARS-CoV-2 genome data also shows that some of the sites

- 24 playing key roles in the virus's fitness and immune escape capability are detected by the
- 25 method.
- 26 The new statistic, called J_{HAC} , is incorporated into the iHDSel software available at
- 27 <https://acraaj.webs.uvigo.es/iHDSel.html>.

28 **Introduction**

29 Evolutionary biology studies the factors that affect genetic variability in populations and
30 species. The main processes that influence the evolution of this variability include mutation
31 and recombination, genetic drift, migration, and natural selection. Natural selection, in
32 addition to affecting the allele carrying a beneficial mutation, impacts the neutral alleles of
33 loci linked to the selective one, producing what is known as genetic hitchhiking (Smith and
34 Haigh 1974; Kaplan et al. 1989), which leads to a selective sweep (Berry et al. 1991; Stephan
35 2019), meaning a loss of diversity around the selected site. These sweeps can be complete or
36 incomplete, strong or soft, and they can even overlap (Johri, Stephan, et al. 2022). Regarding
37 the detection of the footprint left by selective sweeps in genomes, from the earliest methods
38 that explored haplotype patterns, whether by studying homozygosity (Sabeti et al. 2007), its
39 diversity (Kimura et al. 2007), or interpopulation differentiation (Chen et al. 2010), among
40 others, a great number of methods have been developed and continue to be developed.
41 Significant advancements have been made, including the use of summary statistics, the
42 combination of different statistical strategies, and the incorporation of artificial intelligence-
43 based methods (Horscroft et al. 2019; Stephan 2019; Abondio et al. 2022; Arnab et al. 2023;
44 Panigrahi et al. 2023; Whitehouse and Schrider 2023).

45 Methods for detecting selective sweeps require the existence of haplotypic data. Despite
46 improvements in the efficiency and accuracy of methods for estimating haplotypes
47 (Delaneau et al. 2019; Meier et al. 2021; Shipilina et al. 2023), in non-model species
48 (understood as those in which, whether or not a genome has been sequenced, it is poorly

49 annotated and has not traditionally been a model species in the pre-genomic era),
50 haplotype-based detection methods are still not widely used. Instead, it is more common to
51 use interpopulation methods based on detecting molecular markers with excessively high
52 differentiation values, known as "outliers". But even in the case of model species, the use of
53 haplotype-based methods to detect selective sweeps presents the problem that the same
54 genomic pattern that could be produced by a selective sweep could also be explained under
55 different scenarios related to factors as diverse as the quality and characteristics of the
56 sampled data, biological characteristics related to mutation and recombination rates, as well
57 as demographic history and the effects of purifying and background selection (Johri,
58 Aquadro, et al. 2022; Soni et al. 2023; Soni and Jensen 2024).

59 Part of this problem arises from the lack of knowledge of the null distribution of the statistics
60 used, which requires simulating the neutral biological scenario. But overall, it is clear that
61 although a statistical tool can detect a specific genomic pattern in the data, it is unlikely that
62 that pattern could be due solely to the effect of a selective scan. It may do so in some
63 scenarios, but not in others. Therefore, to validate a candidate SNP or region as a result of a
64 selective process, it is first necessary to prove that the statistic does not generate false
65 positives in realistic scenarios in terms of demography and other evolutionary parameters of
66 interest. Subsequently, functional validation of these candidate loci will always be necessary
67 (Johri, Aquadro, et al. 2022). This does not preclude that the development of statistical tools
68 to detect genomic patterns that may be related to selective sweeps remains of great
69 interest. It would also be interesting if that statistic had a known null distribution.

70 When studying a selective sweep, we can trace its effect over time (directional selection) or
71 across space (divergent selection). Therefore, if we use two samples to compare the effect of
72 the sweep, they can be separated by time or space. Detecting the footprint of natural
73 selection in genomes in general, and specifically divergent selection, is important for
74 studying speciation processes (Galindo et al. 2021) and climate adaptation (Folkertsma et al.
75 2024), but also for more immediate effects such as resistance to infections in commercially
76 important marine species (Pampín et al. 2023; Vera et al. 2023).

77 In this work, I propose a statistic that uses the population stability index, also known as
78 Jeffreys divergence, to compare the distribution of allelic classes of haplotypes (Labuda et al.
79 2007; Hussin et al. 2010) between two populations or samples. To develop the statistic I use
80 the informational interpretation of the Price equation (Price 1972; Frank 2012a) defined for
81 the haplotype allelic class trait. The advantage of this statistic is that it follows a chi-square
82 distribution when the null hypothesis (equal distribution of haplotype classes among
83 samples) is true. This not only increases computational efficiency by several orders of
84 magnitude but also allows for the testing of biological models expected to deviate from this
85 hypothesis, including the presence of local selection and its corresponding selective sweep.
86 Below, I will present the development of the statistic and then demonstrate its behavior
87 with both simulated and real genomic data from various samples of the SARS-CoV-2 virus.

88 **The Price equation and the population stability index to compare** 89 **population genomes**

90 **Price equation**

91 The Price equation in its most general formulation describes the change between two
92 populations at any scale, spatial or temporal (Frank 2012a; Frank 2017). The equation
93 partitions the change into a part due to natural selection and another part due to other
94 effects. We compare two populations or frequency distributions which can be separated by
95 space and/or time. Natural selection causes populations to accumulate information, which is
96 measured in relation to the logarithm of biological fitness $m = \log(\omega)$, where ω is the relative
97 fitness (Frank 2012b; Frank 2012a).

98 Therefore, let z be a character that takes different values z_i with associated frequency p_i in
99 population P and with frequency q_i in population Q . If we consider the logarithm of fitness as
100 the character, $z=m$, we have that the mean change in m due to the effect of natural selection
101 in one or the other population is (Frank 2012a)

$$102 \quad \Delta_s \bar{m} = J(p, q) = \beta_{mw} D_w \text{ where } D_w = \frac{V_w}{\bar{w}} \quad (1)$$

103 where J is the Jeffreys divergence or population stability index, p and q the frequency of the
104 different values of m in the populations P and Q respectively, and β_{mw} is the regression of m
105 on the absolute fitness w .

106 However, it is possible to use scales other than the fitness logarithm to measure
107 information, with the key element being the regression of values in the new scale on fitness

108 (Frank 2013). Therefore, to detect the effect of natural selection from genomic data, it will
109 be necessary to measure those genomic patterns with high regression values on biological
110 fitness. In this work, we propose the haplotype allelic class (HAC) as a suitable pattern to
111 capture the increase in information generated by natural selection, whether in temporal
112 comparisons (directional selection) or spatial comparisons (divergent selection).

113 **Haplotype allelic class (HAC)**

114 Haplotype allelic classes were initially introduced in (Labuda et al. 2007) and later used to
115 detect genomic patterns caused by selective sweeps (Hussin et al. 2010) and divergent
116 selection (Carvajal-Rodríguez 2017).

117 Consider a sample of sequences and compute the reference haplotype R as the one formed
118 by the major allele of each site. Now, consider for the same or another sample of sequences,
119 the haplotypes of length $L+1$ centered in a given candidate SNP c and define the mutational
120 distance between any haplotype and the reference R as the Hamming distance between the
121 haplotype and the reference i.e. the number h of sites in the haplotype carrying an allele
122 different to the one in R . Each group of haplotypes having the same h will constitute an
123 haplotype allelic class (HAC, Labuda et al. 2007; Hussin et al. 2010). The HAC distribution is
124 estimated from the distribution of the h values in a sample.

125 Thus, in a given haplotype with the candidate SNP position c in the middle, for each position
126 other than c we count the outcome $X_k = I(s_k \neq r_k)$ where s_k is the allele in the position k of the
127 haplotype, r_k is the allele in the reference and $I(A)$ is the indicator variable taking 1 if A is true
128 and 0 otherwise. Therefore, the h value of an haplotype of length $L+1$ is

129
$$h = \sum_{k=1}^{L+1} X_k \quad \text{where } k \neq c, X_k = I(s_k \neq r_k) \text{ and } h \in [0, L] \quad (2)$$

130 The idea behind using h -values to detect selective sweeps is that if one allele increases in
131 frequency due to the effect of selection, the higher frequency alleles from adjacent sites will
132 be swept along with the selected allele so that these haplotypes will have many common
133 alleles with the reference configuration, i.e., an h -value close to zero.

134 **Information for haplotype allelic classes: the population stability index**

135 Let h_i be the HAC value that satisfies $h=i$ with $i \in [0, L]$ then for a sample of n_1 sequences in
136 P , the frequency of h_i is

137
$$P_i = \# h_i / n_1 \quad \text{with} \quad \sum_i P_i = 1$$

138 similarly, for a sample of n_2 sequences in Q , the frequency of h_i is

139
$$Q_i = \# h_i / n_2 \quad \text{with} \quad \sum_i Q_i = 1$$

140 In previous works, studying the distribution of alleles around a candidate site in both
141 samples P and Q , has been performed comparing in several ways the HAC variances of the
142 partitions that have the reference allele or not in the different samples (Carvajal-Rodríguez
143 2017; Gabián et al. 2022). There are some problems with this type of approach as the
144 unknown distribution of the defined statistics or a loss of power when using homogeneity
145 variance tests. Here, I rely on the abstract model of the Price equation as proposed by Frank
146 (Frank 2012a; Frank 2013; Frank 2017; Frank 2020) to calculate, using Jeffreys divergence,
147 the change caused by selection in the distribution of HAC values between two populations.

148 *Number of classes and smoothing*

149 For a total of $L+1$ different classes the Jeffreys divergence is (Kullback 1997)

$$J_{HAC} = \frac{n_1 n_2}{n_1 + n_2} \sum_{i=0}^L (P_i - Q_i) \ln \frac{P_i}{Q_i}$$

150 However, computing J_{HAC} in this way could suffer from the curse of dimensionality if

151 eventually $L > n_1 + n_2$ which will cause the presence of the different classes to be scarce. To

152 alleviate this problem we will group the values in K ($K \leq L$) HAC classes. The number of classes

153 K is an important parameter because too many classes have the dimensionality issue but too

154 few classes will have low power for the distribution comparison. A heuristic conservative

155 guess is $K=L/2$ when $L \geq 15$ or $K=L$ otherwise.

156 Given K , we will group uniformly the h values into K groups so that the first group indicates

157 classes with less than $(100/K)\%$ of minor alleles, the next corresponds to classes with more

158 than $(100/K)\%$ but less than $2 \times (100/K)\%$, until the last group with more than $(K-1) \times (100/K)\%$

159 but equal or less than 100%. The class with 100% of minor alleles is included in this last

160 group.

161 Thus, for population P , the frequency P'_i of each group of classes is

$$162 \begin{cases} S_i = \sum_{j=u}^U \# h_{j-1} / n_1 \text{ where } i \in [0, K], u = 1 + \frac{L}{K} i \text{ and } U = \frac{L}{K} (i+1) \\ i \in [0, K-1]: P'_i = S_i \\ i = K: P'_K = S_K + \# h_L / n_1 \end{cases} \quad (3)$$

163 However, note that the Jeffreys divergence is defined only if P and Q have no zeros. To avoid

164 zeros we use additive smoothing (Manning et al. 2008) with a pseudocount $\alpha=0.5$ for each

165 possible outcome so that S_i and P'_k in (3) become

$$S_i = \sum_{j=u}^U (\# h_{j-1} + \alpha) / (n_1 + \alpha K)$$

$$P'_k = S_K + (\# h_L + \alpha) / (n_1 + \alpha K)$$

166 So, for K groups of HAC classes, the Jeffreys divergence for comparing the HAC distribution

167 between populations P and Q finally is (c.f. eq. 5.10 in Kullback 1997 p. 130)

168
$$J_{HAC} = \frac{n_1 n_2}{n_1 + n_2} \sum_{i=0}^K (P'_i - Q'_i) \ln \frac{P'_i}{Q'_i} \text{ with values in } [0, +\infty) \text{ (4)}$$

169 Note that J_{HAC} is also known as the population stability index and is asymptotically distributed

170 as Chi-square with $K-1$ degrees of freedom.

171 The advantage of using (4) in the context of studying the genomic footprint of selection is

172 that, contrary to other statistics, it can be approached by a chi-square distribution providing

173 a faster approach as we can avoid performing computationally expensive simulations or

174 resampling.

175 **Phenotypic scale, linkage disequilibrium and window size**

176 **Phenotypic scale**

177 The gain in information caused by the effect of natural selection as expressed in (1) depends

178 on the log-fitness m and if we measure the frequency of the h_i classes instead of fitness

179 classes, the relationship between the average change in the h distribution and the gain in

180 information will depend on the regression of h -values on fitness as follows (Frank 2013)

$$\Delta_s \bar{h} = \beta_{hw} D_w \text{ where } D_w = \frac{V_w}{\bar{w}}$$

181 thus, if we use the HAC values to compute J we obtain J_{HAC}

$$J_{HAC} = \beta_{hw} D_w = \frac{\beta_{hw}}{\beta_{mw}} J$$

182 The quantity β_{hw}/β_{mw} is the change in phenotype (HAC values) relative to the change in
183 information (Frank 2013). Therefore, if there is perfect fit between $\ln(P/Q)$ and m then $J_{HAC}=J$.

184 The regression of h on w will be high when it is fitness that is distributing the classes of h ,
185 which requires that there are indeed one or more sites under selection within the haplotype
186 window. However, this is a necessary but not sufficient condition. Price's equation for total
187 change indicates that the average variation in phenotype h has two components: one due to
188 selection and the other due to other causes, including changes in the components of the
189 phenotype that are transmitted (Δh)

$$\Delta \bar{h} = \Delta_s \bar{h} + q' \Delta h$$

190 In our context, the change in h not caused by selection may be due to, besides mutation, the
191 effect of recombination on haplotypes, which in turn will depend on the window size.
192 Therefore, we are interested in using window sizes that correspond to haplotype blocks in
193 order to minimize Δh .

194 **Window size**

195 The program computes haplotype blocks and set the candidate position c in the middle of
196 each block. An haplotype block is computed as a sequence of reference SNPs with length W

197 that satisfies $r^2(c-W/2, c-W/2+1), \dots, r^2(c-1, c), r^2(c, c+1), r^2(c+x-1, c+x), \dots, r^2(c+W/2-1, c+W/2), \dots$
198 where r is the correlation coefficient calculated from the sample of size n so that $Pr(nr^2) \leq \alpha$
199 and nr^2 has a Chi square distribution. Furthermore, for a given SNP $c+1$ to be included in the
200 block, it is also required that $D'(c, c+1) \geq 0.4$, where D' is the normalized linkage disequilibrium
201 (Lewontin 1964). The block is extended until any of both conditions is rejected i.e. $Pr(nr^2_{c+x-1, c+x}) > \alpha$
202 or $D'(c+x-1, c+x) < 0.4$.

203 Optionally, the program can use an outlier as the putative center of a block and build the
204 block around it. In this case, the condition for defining a block is more liberal, allowing blocks
205 that have a mean normalized linkage disequilibrium value greater than zero. The reason is
206 that the outliers may have been part of older blocks, so we use the minimum condition that
207 the average linkage of reference alleles is greater than zero assuming that, if they are not the
208 product of selective sweep, the distribution of haplotypic classes will not be affected, the
209 latter will be checked in the next section by simulation.

210 **Simulations**

211 The same simulated data as in (Carvajal-Rodríguez 2017; Gabián et al. 2022) were used. Two
212 populations of 1000 facultative hermaphrodites were simulated under divergent selection
213 and different conditions about mutation, recombination, migration and selection. Each
214 individual consisted of a diploid chromosome of length 1Mb.

215 **Input setting for the simulations**

216 A minor allele frequency (MAF) value of 0.01 was used. As we have already seen, the
217 program allows defining the window or haplotypic block size automatically, using the

218 correlation between pairs of sites to define the block size and placing the central SNP as a
219 candidate or, alternatively, it uses the detected outliers as candidate SNPs and then
220 calculates the window size. Both methods were used. All other parameters were as defined
221 by default (see the program manual). An example of the command line to launch case C1
222 (Table 1) and analyze the 1,000 files located in subfolder C1 and using the automatic
223 calculation of blocks (-useblocks 1) is:

```
224 -path /home/data/C1/ -runs 1000 -input Om_SNPFile_Run -format ms -sample 50  
225 -minwin 11 -output JHAC_C1_ -maf 0.01 -useblocks 1 -doEOS 1 &
```

226 The -doEOS tag indicates whether we want (1, default) or not (0) to run in addition the EOS
227 outlier test (Carvajal-Rodríguez 2017). If the calculation without blocks is used (-useblocks 0)
228 the doEOS tag must necessarily be set to 1.

229 **Simulation results**

230 In the following tables the results of power (Tables 1-3) and false positive rate (Table 4) after
231 analyzing 1000 replicates of each scenario are presented. In summary, for haplotypes with
232 linkage and the selective site in the center of the chromosome, when using the automatic
233 blocks system, the power is equal to or greater than 95%, regardless of mutation and
234 recombination rates. As expected, if the sites are not linked, the method does not work
235 because there is no selective sweep (Table 1). When the position of the selective site moves
236 away from the center of the chromosome (Table 2), the power remains high. Localization
237 improves as recombination increases and as the marker is located closer to the center. In the
238 case of multiple selective sites (Table 3), the power to detect at least three is above 75%
239 when using automatic blocks but only detects one (97% power) in the case of blocks

240 centered on outliers. In general, for blocks centered on outliers, the power is slightly lower,
 241 but in some cases, the localization was considerably more accurate.

242 **Table 1. Percent power for detecting divergent selection by J_{Hac} in simulated data with the selective site in**
 243 **the middle. The power was computed as 100×the number of replicates where selection was detected/1000.**
 244 **In parentheses, the corresponding value when the blocks were built around outliers instead of finding the**
 245 **blocks automatically, if the value is equal the = symbol appears. Genome size is 1Mb. Population size $N=$**
 246 **1000. T : number of generations. Population mutation rate $\theta = 4N\mu$. Population recombination rate $\rho =$**
 247 **$4Nr$. s : selection coefficient. $Dist$: average distance in Kb from the detected position to the actual effect,**
 248 **given only when $\rho>0$. W : average size, in number of SNPs, of the haplotypes analyzed. Significance level α**
 249 **= 0.05. Each case was replicated 1,000 times.**

Case	T	θ	ρ	s	% power	Dist Kb	W
C1	10^4	12	0	± 0.15	100 (98)	-	14 (13)
C2	10^4	12	4	± 0.15	100 (98)	42 (38)	14 (13)
C3	10^4	12	12	± 0.15	100 (96)	4 (10)	13 (12)
C7	5×10^3	60	0	± 0.15	100 (94)	-	13 (12)
C8	5×10^3	60	4	± 0.15	100 (85)	37 (14)	13 (12)
C9	5×10^3	60	60	± 0.15	98 (80)	14 (2)	12 (11)
C13	10^4	60	0	± 0.15	100 (100)	-	14 (=)
C14	10^4	60	4	± 0.15	99 (100)	126 (15)	14 (13)
C15	10^4	60	60	± 0.15	95 (91)	19 (2)	13 (12)
C15Indep	10^4	60	∞	± 0.15	0 (2*)	- (-)	- (11)

250 * Note that this 2% results from using the outlier-centered haplotype method. When directly inspecting outliers with the EOS
 251 method, the power was 78%.

252 **Table 2. Percent power for detecting divergent selection by J_{Hac} in simulated data with the selective site in**
 253 **different locations. The power was computed as 100×the number of replicates where selection was**
 254 **detected/1000. In parentheses, the corresponding value when the blocks were built around outliers instead**
 255 **of finding the blocks automatically, if the value is equal the = symbol appears. Genome size is 1Mb.**
 256 **Population size $N=$ 1000. T : number of generations. Population mutation rate $\theta = 4N\mu$. Population**
 257 **recombination rate $\rho = 4Nr$. s : selection coefficient. Loc : true relative position of the selective site. $Dist$:**
 258 **average distance in Kb from the detected position to the actual effect, given only when $\rho>0$. W : average**
 259 **size, in number of SNPs, of the haplotypes analyzed. Significance level $\alpha = 0.05$. Each case was replicated**
 260 **1,000 times.**

Case	T	θ	ρ	s	Loc	% power	Dist Kb	W
C13loc0	10^4	60	0	± 0.15	0.0	100 (99)	-	14 (13)
C13loc10	10^4	60	0	± 0.15	0.01	100 (99)	-	14 (13)
C13loc100	10^4	60	0	± 0.15	0.1	100 (98)	-	14 (13)

C13loc250	10^4	60	0	± 0.15	0.25	100 (99)	-	14 (13)
C14loc0	10^4	60	4	± 0.15	0.0	98 (93)	300 (262)	14 (13)
C14loc10	10^4	60	4	± 0.15	0.01	98 (96)	285 (292)	14 (13)
C14loc100	10^4	60	4	± 0.15	0.1	99 (96)	180 (229)	14 (13)
C14loc250	10^4	60	4	± 0.15	0.25	99 (98)	62 (114*)	14 (14)
C15loc0	10^4	60	60	± 0.15	0.0	86 (79)	211 (189)	13 (11)
C15loc10	10^4	60	60	± 0.15	0.01	87 (80)	198 (170)	13 (11)
C15loc100	10^4	60	60	± 0.15	0.1	91 (89)	106 (70)	13 (12)
C15loc250	10^4	60	60	± 0.15	0.25	92 (89)	37 (14)	13 (12)

261 * Several runs with average $F_{ST} > 0.5$ and no outliers, so the 90th percentile was considered.

262 **Table 3. Percent power for detecting divergent selection by J_{Hac} in simulated data for a polygenic model**
 263 **with 5 selective sites uniformly distributed in the chromosome. The power was computed as the number of**
 264 **replicates where selection was detected. In parentheses the corresponding % power when the blocks were**
 265 **built around outliers instead of finding the blocks automatically, if the value is equal the = symbol**
 266 **appears. Genome size is 1Mb. Population size $N=1000$. Number of generations $T=10^4$. Population**
 267 **mutation rate $\theta = 4N\mu=60$. Population recombination rate $\rho = 4Nr=60$. Selection coefficient per site $s=\pm$**
 268 **0.032. W : average size, in number of SNPs, of the haplotypes analyzed. Each case was replicated 100**
 269 **times.**

Case	Candidate	% power	W
C15poly	1	99 (97)	15 (18)
C15poly	2	89 (0)	16
C15poly	3	75 (0)	16
C15poly	4	59 (0)	16
C15poly	5	44 (0)	16

270 Finally, in the neutral simulations where there was no selective site (Table 4), the false
 271 positive rate conservatively remains below the expected 5%, both using automatic blocks
 272 and those centered on outliers, with one exception corresponding to the effect of
 273 bottlenecks. When a bottleneck occurs, it can generate linkage disequilibrium that could
 274 resemble the effect of a selective sweep, thus increasing the possibility of false positives. In
 275 our case, we observed that J_{Hac} becomes liberal with 13% when the blocks are centered

276 around the outliers, which means an 8% excess over the expectation. The explanation for
 277 this happening with blocks centered on outliers but not with automatic ones is that, as
 278 previously indicated, the construction of blocks centered on outliers is somewhat more
 279 liberal, validating as blocks those regions that have an average disequilibrium greater than 0.
 280 A conservative option available for the above exception is to set the window size to a higher
 281 value, say 25 or 50, which solves the problem and sets the false positive rate to just 2%.
 282 While for the corresponding selective case when we run the program with these window
 283 sizes the power is 90%.

284 **Table 4. Percent false positive rate for detecting divergent selection in simulated neutral data. In**
 285 **parentheses the corresponding value when the blocks were built around outliers instead of finding the**
 286 **blocks automatically, if the value is equal the = symbol appears. Genome size is 1Mb. Population size $N=$**
 287 **1000. T : number of generations. Population mutation rate $\theta = 4N\mu$. Population recombination rate $\rho =$**
 288 **$4Nr$. %FPR = $100 \times$ number of replicates with significant J_{Hac} test/1000. W : average size, in number of**
 289 **SNPs, of the haplotypes analyzed. Each case was replicated 1,000 times.**

Case	T	θ	ρ	% FPR	W
C4	10^4	12	0	0.1 (1)	11 (=)
C5	10^4	12	4	0.3 (2)	12 (11)
C6	10^4	12	12	0.1 (4)	12 (11)
C10	5×10^3	60	0	0 (0.4)	- (11)
C11	5×10^3	60	4	0 (2)	- (11)
C12	5×10^3	60	60	0.2 (3)	12 (11)
C16	10^4	60	0	0.3 (0.4)	12 (11)
C17	10^4	60	4	1 (2)	12 (11)
C18	10^4	60	60	1 (4)	13 (=)
C18Indep	10^4	60	∞	0 (0.2)	- (11)
C18Bottle	10^4	60	60	3 (13)	12 (11)
C18Bottle	10^4	60	60	2	26*
C18Bottle	10^4	60	60	2	51*

290 * window size set to a specific value

291 **Real data analysis: SARS-CoV-2**

292 SARS-CoV-2 virus genomes stored in the GISAID database (Khare et al. 2021) are indexed by
293 both locality and the time period where they were sampled thus presenting a unique
294 opportunity to apply iHDSel to both time or spatially separated samples. Therefore, as an
295 example of application, we are going to compare SARS-CoV-2 genomes sampled in Spain
296 (SP), England (EN) and South Africa (SA) in periods corresponding to different waves. The
297 findings of this section are based on data associated with 30,274 SARS-CoV-2 genomes
298 available on GISAID up to February 12, 2024, gisaid.org/EN1, gisaid.org/EN2, gisaid.org/EN3,
299 gisaid.org/EN4, gisaid.org/SP1, gisaid.org/SP2, gisaid.org/SA.

300 The downloaded genomes were complete (>29,000 bp) and of high quality (<1% undefined
301 bases and <0.05% unique amino acid mutations). These datasets were then processed using
302 the Nextclade CLI for quality control (Aksamentov et al. 2021). Briefly, the Nextclade CLI
303 examines the completeness, divergence, and ambiguity of bases in each genome. Only
304 genomes considered 'good' by Nextclade CLI were selected.

305 The samples from England (EN1, EN2, EN3 and EN4) correspond to the period of March 2020,
306 at the beginning of the first wave of the pandemic (EN1, 4820 genomes collapsed to 4227
307 after quality control), a second sample taken between March 28 and March 31, 2021,
308 inclusive (EN2, 5966 genomes collapsed to 4152 after quality control), a third from June 24
309 to June 26, 2021, inclusive (EN3, 6886 genomes collapsed to 5844 after quality control), and

310 from October 1, 2023, until January 31, 2024, inclusive (EN4, 3928 genomes collapsed to
311 3712 after quality control).

312 The samples from Spain (SP1 and SP2) correspond to the periods June 24, 2021, to July 12,
313 2021, inclusive (SP1, 6195 genomes collapsed to 4627 after quality control) and October 1,
314 2023, to January 31, 2024, inclusive (SP2, 1012 genomes collapsed to 221 after quality
315 control).

316 Finally, the sample from South Africa corresponds to the same period as SP1, June 24, 2021
317 to July 12, 2021, inclusive (SA, 1467 genomes collapsed to 1327 after quality control).

318 These samples will allow us to compare population changes in space or time. We will
319 compare genomes from different samples to study if there are genomic patterns that the J_{HAC}
320 test identifies as potentially caused by selection (see below).

321 **Rationale of the comparisons**

322 *Spatial comparisons: SP1-SA, EN3-SA, EN3-SP1*

323 These comparisons involve samples from different countries obtained in the same time
324 period of the pandemic. The interest in the comparison with South Africa is that on June 24,
325 2021 to July 12, 2021, vaccination rates were high in Spain and England but very low in South
326 Africa. Virtually 100% of the Spanish and English population was vaccinated with at least one
327 dose and less than 10% of the South African population ([https://ourworldindata.org/covid-](https://ourworldindata.org/covid-vaccinations?country=ZAF)
328 [vaccinations?country=ZAF](https://ourworldindata.org/covid-vaccinations?country=ZAF)).

329 *Temporal comparisons: EN1-EN2, EN2-EN3, EN3-EN4*

330 These comparisons affect the same country but in different periods of the pandemic from
331 the beginning of the first wave to the beginning of 2024 with virtually the entire population
332 already vaccinated several times and the majority variant being Omicron and its subvariants
333 (Brüssow 2022; Wang et al. 2023; Wang et al. 2024).

334 *Spatial comparisons: EN4-SP2*

335 At the end of 2023, the JN.1 subvariant of Omicron, originating from the BA.2.86 lineage,
336 began to spread. This subvariant already carried more than 30 mutations in the spike protein
337 compared to previous subvariants. JN.1 includes the L455S mutation and, by the end of
338 2023, exhibited a higher reproductive rate than previous sublineages in countries such as
339 Spain, France, and England, with the number of detected JN.1 sequences being higher in
340 England than in Spain (Kaku et al. 2024). During this period, DV.7.1, a sub-lineage of BA.2.75,
341 was highly prevalent in Spain (50% compared to 5% in the UK,
342 https://cov-lineages.org/lineage_list.html) and was considered a variant to monitor,
343 although it was later downgraded. Therefore, the comparison between EN4 and SP2,
344 corresponding to October 2023 - January 2024, is of interest to study the potential patterns
345 of divergent selection in the evolutionary dynamics of Omicron subvariants between these
346 two countries.

347 **Genome alignment and lineage classification**

348 The pooled genomes for each comparison were aligned with the MAFFT FFT-NS-2 program
349 (Katoh and Standley, 2013) with the specific version for SARS-CoV-2 accessible online
350 (https://mafft.cbrc.jp/alignment/server/add_sarscov2.html). Sequences that had more than

351 5% ambiguous sites were removed and also, to keep the alignment length the same as the
352 input, insertions were deleted. The remaining options were the default. After the alignment,
353 and following the protocol recommended by NextStrain given the possibility of artifactual
354 SNPs located at the beginning and end of the alignment (van Dorp et al. 2020), sites in the
355 first 130 base pairs and the last 50 were removed using the program Mega X (Kumar et al.
356 2018). Lineages were identified with Nextclade CLI (Table 5).

357 **Table 5. Percentage of SARS-CoV-2 lineages in the analyzed data.**

Data	%Alpha	%Beta	%Delta (%AY.4/AY.45)	%Gamma	%Omicron (%JN.1/FLIP/DV.7.1)	%Other (pre-Alpha, Lambda, Mu, recombinants, undefined)
SP1	24	2	70 (2/0)	2	0	2
SA	1	3	94 (0/57)	0	0	2
EN1	0	0	0	0	0	100 (pre-Alpha)
EN2	98	1	0.1	0.1	0	0.8
EN3	1	0.02	98.9 (72/0)	0	0	0.08
EN4	0	0	0	0	96 (39/6/1)	4 (recombinants)
SP2	0	0	0	0	97 (26/12/28)	3 (recombinants)

358 **Input settings for iHDSel**

359 A minor allele frequency (MAF) value of 0.01 was used. The two methods already mentioned
360 were used to define the window size (automatic or outlier-centered blocks) and the results
361 detected by either of the two methods are reported. All other parameters were the ones by
362 default (see program manual). An example of the command line for the comparison
363 between EN3 and SP1 where both samples are in the file EN3_SP1.fas located in the data
364 folder and using the outlier-centered block calculation (-useblocks 0) is:

```
365 -path /home/data/ -input EN3_SP1.fas -format fasta -output EN3_SP1 -  
366 useblocks 0 -tag ENGLAND &
```

367 where *-tag* is the argument that defines the word included in the name from the England
368 sequences and that allows to separate both samples.

369 Similarly, for the temporal comparison between EN2 and EN3

```
370 -path /home/data/ -input EN2_EN3.fas -runs 1 -format fasta -output EN2_EN3  
371 -useblocks 0 -tag 2021-03 -reference 2
```

372 where we have added the *-reference* tag to indicate that the EN3 sample should be used as a
373 sample to calculate the blocks and the reference haplotype.

374 **The imprint of selection in the SARS-CoV-2 genomes**

375 *Spatial comparisons: SP1-SA (summer 2021)*

376 The SP1 sample has a majority Delta (70%) and Alpha (24%) composition while SA is mostly
377 (94%) Delta (Table 5). The pooled SP1-SA sample consists of 247 SNPs with a frequency
378 greater than 1%. After genome-wide analysis, iHDSel did not find any significant haplotypic
379 blocks in the automatic search nor when focusing on outliers.

380 *Spatial comparisons: EN3-SA (summer 2021)*

381 Both samples are mostly Delta (99% EN3 and 94% SA, Table 5). The pooled EN3-SA sample
382 consists of 107 SNPs with a frequency higher than 1%. After whole genome analysis, iHDSel
383 found one site with the automatic block method (28,282) and five sites centered on outliers
384 (Table 6).

385 The first site is 7,851, which corresponds to ORF1a 2,529. In the SA sample, 100% of the
386 sequences have the amino acid A, while in EN3, there is 27%A and 73%V, indicating the
387 change A2529V. It is noteworthy that A2529V is one of the main SARS-CoV-2 mutations
388 associated with virus fitness (Jankowiak et al. 2022). Moreover, in a recent study (Garcia et
389 al. 2024) analyzing the evolution of different lineages in relation to the progress of
390 vaccination, the A2529V mutation in ORF1a showed a significant positive correlation

391 between the prevalence of the mutation and vaccination in Norway during the first 9
392 months of 2021 (including the sampling period of EN3 and SA).

393 The second site is 13,812, which, after identifying the slippery region (Kelly et al. 2021) and
394 the start of ORF1b at 13,468, corresponds to amino acid 115 in ORF1b (NSP12). This site has
395 100%M in EN3 but 42%M and 58%I in SA. The change M115I is a characteristic mutation of
396 the AY.45 lineage (Gangavarapu et al. 2023), which is present in SA with a frequency of 57%
397 but is absent in EN3.

398 The third and fourth sites are mutations corresponding to amino acid changes in the Spike
399 protein. Specifically, T95I represents the change observed between SA and EN3, with I at a
400 frequency of only 8% in SA but 72% in EN3. The other mutation in Spike is G142D, with D
401 present at 62% in SA and 97% in EN3 (Table 6). Both mutations are characteristic of the Delta
402 variants and increase in frequency in Delta Plus (Cai and Cai 2021; Dhawan et al. 2022;
403 Kannan et al. 2022; Mahmood et al. 2022).

404 The fifth site is position 25,413 of the genome, corresponding to amino acid 7 in ORF3a, with
405 amino acid I in both samples being EN3 (ATC) and SA (ATT|50%C). Therefore, the existence
406 of a significant signal due to different HAC distribution must be caused by accumulated
407 variation in the surrounding sites. Similarly, the sixth and final site corresponds to amino acid
408 3 of the N protein, with the amino acid being D (GAT) in 99% of the cases in both samples,
409 with practically 1% being L (CTA). Again, the existence of a significant signal due to different
410 HAC distribution is caused by accumulated variation in the surrounding sites.

411 **Table 6. Significant J_{Hac} tests ($p\text{-val}<0.05$) for EN3-SA comparison (with 107 SNPs and sample sizes $n_{EN3} =$
412 5844 , $n_{SA}=1327$).**

EN3-SA		Gene (protein)	AA		%
Block size	Site (+1+130)		(AA in EN3)	(AA in SA)	
41	7851	ORF1a (NSP3)	(V A) 2529 (A)		(73 27):(- 100)
11	13812	ORF1b (NSP12)	(M) 115 (M I)		(100):(42 58)
30	21846	ORF2 (S)	(I T) 95 (I T)		(76 24):(8 92)
14	21987	ORF2 (S)	(D G) 142 (D G)		(97 3):(62 38)

11	25413	ORF3a	(I) 7 (I)	(100):(100)
14	28282	ORF9 (N)	(D L) 3 (D L)	(99 1):(99 1)

413 (+1+130): added to the program output position, the +1 to correct the program indexing to 0 and the +130 to correct the eliminated initial
414 positions.

415 *Spatial comparisons: EN3-SP1 (summer 2021)*

416 We already saw that the EN3 genomes are predominantly Delta (99%), while SP1 has 70%
417 Delta genomes and 24% Alpha (Table 5). The combined EN3-SP1 sample consists of 154 SNPs
418 with a frequency greater than 1%. After the whole genome analysis, iHDSel found one
419 significant site. The nucleotide site 7851 corresponds to amino acid 2,529 in ORF1a, which
420 was also significant in the EN3-SA comparison, and we saw that A2529V is one of the main
421 SARS-CoV-2 mutations associated with virus fitness. In this comparison, the change is from
422 98%A in SP1 to 73%V (27%A) in EN3.

423 Therefore, regarding the spatial comparisons in the summer of 2021, we see that in the SA
424 and SP1 samples, amino acid 2529 of ORF1a was still A in virtually 100% of the sequences
425 analyzed, while in EN3, only 27% had A and the remaining 73% were already V. This
426 mutation is associated with an advantage for the virus and in relation to vaccination, and
427 indeed, the J_{HAC} statistic detects it as a site with a selective pattern.

428 *Temporal comparisons: EN1-EN2 (March 2020 vs March 2021)*

429 The comparison between the English genomes is between samples separated in time
430 (different waves). These comparisons should be considered with caution as the
431 differentiation between samples is very large. Indeed, the mean F_{ST} in all three comparisons
432 (EN1-EN2, EN2-EN3 and EN3-EN4) is above 0.5. However, the sites detected in the three

433 comparisons correspond to sites with recognized impact on virus fitness.

434 The genomes in EN1 belong to pre-alpha variants, while the genomes in EN2 are Alpha. The
 435 combined EN1-EN2 sample consists of 77 SNPs with a frequency greater than 1%. After the
 436 whole genome analysis, iHDSel found six significant sites for the J_{HAC} test. These sites
 437 correspond to six Spike mutations, namely amino acids 501, 570, 681, 716, 982, and 1118
 438 (Table 7). All of them correspond to the characteristic Spike mutations of Alpha
 439 (Gangavarapu et al. 2023). The only one missing is D614G, although it is included in the
 440 detected haplotypic regions. The fact that it does not come out as directly significant may be
 441 because the program did not use that position as the center of a haplotypic block, as it
 442 detected the other sites as more extreme outliers since 614G has a presence of 61%G in EN1
 443 and 99.9% in EN2. However, when the program is run proposing the nucleotide positions
 444 corresponding to the amino acid 614 as candidates, the result is significant. Therefore, it
 445 seems that the haplotypic region including all these mutations has been detected.

446 **Table 7. Significant J_{Hac} tests ($p\text{-val}<0.05$) for EN1-EN2 comparison (with 77 SNPs and sample sizes $n_{EN1} =$
 447 4224 , $n_{EN2}=4152$).**

EN1-EN2		Gene (protein)	AA	%
Block size	Site (+1+130)		(AA in EN1) position (AA in EN2)	(p1 p2 ... EN1) : (p1 p2 ... EN2)
11	23063	ORF2 (S)	N501Y	(100):(1 99)
11	23271	ORF2 (S)	A570D	(100):(2 98)
11	23604	ORF2 (S)	P681H	(100):(1 99)
11	23709	ORF2 (S)	T716I	(100):(1 99)
11	24506	ORF2 (S)	S982A	(100):(2 98)
11	24914	ORF2 (S)	D1118H	(100):(1 99)

448 (+1+130): added to the program output position, the +1 to correct the program indexing to 0 and the +130 to correct the eliminated initial
 449 positions.

450 *Temporal comparisons: EN2-EN3 (March 2021 vs June 2021)*

451 This is a comparison of Alpha (EN2) with Delta (EN3) genomes. The pooled EN2-EN3 sample
452 consists of 105 SNPs with a frequency greater than 1%. After whole genome analysis, iHDSel
453 found seven significant sites using blocks centered on outliers (Table 8).

454 These included substitution of relevant Spike amino acids at sites such as 452, 478, 681, and
455 950 (Kannan et al. 2021). For example, the L452R substitution appears to be associated with
456 evasion of the immune response (He et al. 2022). As well as three sites in the N protein, 63,
457 203 and 377, which correspond to significant mutations of the delta variant, namely, D63G,
458 R203M, and D377Y (Bhattacharya et al. 2023).

459 **Table 8. Significant J_{Hac} tests ($p\text{-val}<0.05$) for EN2-EN3 comparison (with 105 SNPs and sample sizes n_{EN2}
460 = 4152, $n_{EN3}=5844$).**

EN2-EN3		Gene (protein)	AA
Block size	Site (+1+130)		(AA in EN2) position (AA in EN3)
18	22917	ORF2 (S)	L452R
18	22995	ORF2 (S)	T478K
13	23604	ORF2 (S)	H681R
12	24410	ORF2 (S)	D950N
12	28461	ORF9 (N)	D63G
11	28881	ORF9 (N)	K203M
13	29402	ORF9 (N)	D377Y

461 (+1+130): added to the program output position, the +1 to correct the program indexing to 0 and the +130 to correct the eliminated initial
462 positions.

463 *Temporal comparisons: EN3-EN4 (June 2021 vs January 2024)*

464 This is a comparison of Delta genomes (EN3) with Omicron genomes (EN4). The pooled EN3-
465 EN4 sample consists of 239 SNPs with a frequency greater than 1%. After whole genome
466 analysis, iHDSel identified several sites with F_{ST} greater than 0.99 and 14 of them in the
467 center of significant blocks (Table 9).

468 The first site occurs in ORF1a (NSP5) and corresponds to the amino acid change P132H,
 469 which is a mutation in a functionally important domain and characteristic of Omicron
 470 (Hossain et al. 2022). The remaining sites presented in Table 9 correspond to core Omicron
 471 mutations in Spike (Basheer et al. 2023; Chen et al. 2023) including some like S371F, S373P,
 472 and S375F, which are related to alterations in binding and entry preference (Hu et al. 2022;
 473 Zheng et al. 2023) and also the 'Kraken' subvariant immune escape F486P (Parums 2023).
 474 Finally, the synonymous change L18L in ORF7b is within the same haplotypic block as the
 475 reversions A82V and I120T in ORF7a, which, when directly contrasted as candidates, were
 476 significant.

477 **Table 9. Significant J_{Hac} tests ($p\text{-val}<0.05$) for the EN3-EN4 comparison (with 239 SNPs and sample sizes**
 478 **$n_{EN3} = 5844$, $n_{EN4} = 3712$).**

EN3-EN4		Gene (protein)	AA
Block size	Site (+1+130)		(AA in EN3) position (AA in SP2)
11	10447	ORF1a (NSP5)	P132H
11	22674	ORF2 (S)	S371F
11	22679	ORF2 (S)	S373P
11	22686	ORF2 (S)	S375F
11	22775	ORF2 (S)	D405N
11	22786	ORF2 (S)	R408S
11	22813	ORF2 (S)	K417N
11	22898	ORF2 (S)	G446S
11	22992	ORF2 (S)	S477N
11	23019	ORF2 (S)	F486P
11	23055	ORF2 (S)	Q498R
11	23075	ORF2 (S)	Y505H
11	25000	ORF2 (S)	D1146D
11	27807	ORF7b	L18L (ORF7a A82V, ORF7a I120T)

479 (+1+130): added to the program output position, the +1 to correct the program indexing to 0 and the +130 to correct the eliminated initial
 480 positions.

481 *Spatial comparisons: EN4-SP2*

482 The genomes of both samples are Omicron but the subvariant composition is different

483 (Table 5). The pooled EN4-SP2 sample consists of 218 SNPs with a frequency greater than
484 1%. After whole genome analysis, iHDSel identified four significant sites (Table 10).

485 The change A427V in ORF1a is characteristic mutation of the DV.7.1 Omicron sublineage
486 (Gangavarapu et al. 2023) which is virtually absent in EN4 (0.6%) but has a 28% in SP2 (Table
487 5) which explains the absence of 427V in EN4 and the 29%V in SP2. The same scenario
488 applies to A520V in ORF1b. The other two significant sites belong to Spike. The mutation at
489 445 would be related to the V445H and V445P changes that seem to favor immune evasion
490 of the virus (Ao et al. 2023; Chen et al. 2023) with the presence of 445V being 30% in SP2 but
491 only 1% in EN4 (Table 10). Finally, L858I is also a characteristic mutation of DV.7.1.

492 **Table 10. Significant J_{Hac} tests ($p\text{-val}<0.05$) for the EN4-SP2 comparison (with 218 SNPs and sample sizes**
493 **$n_{EN4} = 3712$, $n_{SP2}=221$). Only amino acids with a frequency equal or greater than 1% are indicated.**

EN4-SP2		Gene (protein)	AA
Block size	Site (+1+130)		(EN4 AA) position (SP2 AA)
11	1545	ORF1a (NSP2)	A427(71%A 29%V)
13	15026	ORF1b (NSP12)	A520(71%A 29%V)
11	22895	ORF2 (S)	(51%H 47%P 1%V)445(31%H 39%P 30%V)
11	24134	ORF2 (S)	L858(71%L 29%I)

494 (+1+130): added to the program output position, the +1 to correct the program indexing to 0 and the +130 to correct the eliminated initial
495 positions.

496 Discussion

497 In this work, a new statistic called J_{Hac} is proposed to detect genomic patterns compatible
498 with selective sweeps. The statistic is constructed from the interpretation in terms of
499 information of the Price equation (Price 1972; Frank 2012a) and consists of the population
500 stability index applied to the distribution of haplotype classes in two samples. The iHDSel
501 program incorporates the statistic along with the calculation of haplotype blocks in such a
502 way that each candidate site is located in the center of a block. J_{Hac} appears to work

503 optimally with simulated data where two populations are subjected to divergent selection
504 under different mutation and recombination conditions. However, if using the program
505 mode that places the outlier sites in the center of the blocks, care must be taken because
506 the false positive rate increases in bottleneck scenarios. A possible correction in these
507 scenarios is to repeat the calculation with a slightly larger window size.

508 Real SARS-CoV-2 data have also been used to test J_{Hac} in both spatial and temporal
509 comparisons. Some sites known to impact virus fitness and its ability to promote immune
510 escape have been detected.

511 **The Price equation for comparing genomic patterns**

512 The general formulation of the Price equation describes a change between two populations
513 at any scale, spatial or temporal (Frank 2017). The Price equation has been proposed as a
514 unifying principle in evolutionary biology, allowing the formulation and systematization of
515 different evolutionary models and motivating the development of equations and models
516 that reveal invariances and general principles (Luque 2017; Luque and Baravalle 2021). Here,
517 we have used the selective component of the Price equation, specifically its interpretation in
518 terms of information theory (Frank 2012a), which allows the expression of the covariance
519 between fitness and the trait under study in terms of Jeffreys divergence or population
520 stability index. We have defined the trait as the allelic class of haplotypes and used Jeffreys
521 divergence to compare the distribution of the trait between two populations. The change in
522 trait distribution would be compatible with the effect of selective sweeps, whether due to
523 divergent or directional selection, depending on whether we are comparing populations in

524 space or time.

525 **Limitations of the J_{Hac} method**

526 The detection of selective sweeps is affected by different evolutionary and demographic
527 scenarios. Throughout the space of the various parameters (mutation, recombination,
528 background and deleterious selection, etc.) it is not difficult to find scenarios that generate an
529 excess of false positives (Johri, Aquadro, et al. 2022; Soni et al. 2023). In our case, we have
530 seen that some evolutionary scenarios, such as bottlenecks, can generate interpopulation
531 genomic patterns that increase the false positive rate when using automatic window sizes
532 centered on outliers. Although increasing the window size restores control over the false
533 positive rate, it is possible that other scenarios without positive selection could also alter
534 haplotype class patterns.

535 Moreover, as we have already indicated, the method proposed here arises from the
536 informational interpretation of the selective component of the Price equation. However, it is a
537 statistical decomposition based on covariance, and we know that correlation does not imply
538 causation. There is also no a priori guarantee that the partition between selection and
539 transmission is additive (Okasha and Otsuka 2020). Therefore, J_{Hac} is an indirect method that
540 detects a genomic pattern possibly related to selection but which can also be generated under
541 other circumstances. Hence, the detected sites should be verified through direct methods such
542 as the study of gene function, fitness, etc.

543 Finally, some genomic patterns of selection correlate with environmental variables, making it
544 difficult to separate both effects (Folkertsma et al. 2024). The method proposed here could be
545 combined with other methods that take this correlation into account.

546 **Concluding remarks**

547 There are many statistics for identifying regions of selective sweeps in genomes, see for
548 example (Horscroft et al. 2019; Stephan 2019; Horscroft et al. 2020; Abondio et al. 2022;
549 Panigrahi et al. 2023). The use of machine learning-based methods to detect selection
550 patterns has been increasing due to their accuracy and ability to handle large amounts of
551 complex data. The underlying idea of all these methods is to use classification algorithms
552 trained with known response data (simulations). That is, if we aim to detect a selection
553 pattern, we train the algorithm with data that we know contains that pattern and with other
554 data without the pattern. Different types of algorithms have been applied: neural networks,
555 extremely randomized trees, and boosting algorithms (Horscroft et al. 2019; Panigrahi et al.
556 2023). A major advantage of these methods is their power and flexibility, partly due to the
557 ease of incorporating new statistics with minimal changes to the structure of the method.
558 Two recent machine learning methods have been designed to detect genomic signatures
559 caused by natural selection, using a supervised multi-statistic machine learning approach
560 (Arnab et al. 2023; Lauterbur et al. 2023). In this work, we have developed a new statistic,
561 J_{Hac} , which, due to its known null distribution, allows us to efficiently and quite accurately
562 test for the existence of genomic patterns compatible with selective sweeps. Therefore, J_{Hac}
563 could be an additional measure to consider for future AI-based selection detection methods.
564 In addition, J_{Hac} has been incorporated into the iHDSel program
565 (<https://acraaj.webs.uvigo.es/iHDSel.html>) along with an automatic haplotype block
566 detection system, so it can be run independently or in conjunction with the heuristic EOS
567 outlier detection method (Carvajal-Rodríguez 2017).

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