

1 Self-inhibiting percolation and viral 2 spreading in epithelial tissue

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9
10 **Abstract** SARS-CoV-2 induces delayed type-I/III interferon production, allowing it to escape the
11 early innate immune response. The delay has been attributed to a deficiency in the ability of cells
12 to sense viral replication upon infection, which in turn hampers activation of the antiviral state in
13 bystander cells. Here, we introduce a cellular automaton model to investigate the spatiotemporal
14 spreading of viral infection as a function of virus and host-dependent parameters. The model
15 suggests that the considerable person-to-person heterogeneity in SARS-CoV-2 infections is a
16 consequence of high sensitivity to slight variations in biological parameters near a critical
17 threshold. It further suggests that within-host viral proliferation can be curtailed by the presence
18 of remarkably few cells that are primed for IFN production. Thus the observed heterogeneity in
19 defense readiness of cells reflects a remarkably cost-efficient strategy for protection.

21 Introduction

22 Adaptive immune responses are relatively slow since they require pathogen-specific priming of im-
23 mune cells (*Sette and Crotty, 2021*). For example, the time required for the body to activate adap-
24 tive immunity against the SARS-CoV-2 virus upon initial infection is around 10 days, comparable
25 to the delay of immunization against SARS-CoV-2 after vaccination (*Polack et al., 2020*). Instead,
26 the earliest infection dynamics are largely governed locally, by infected cells and their neighbor-
27 hood. The innate responses including both interferon (IFN) mediated intercellular communication
28 and expression of antiviral genes (ISGs) are determinants for confining the viral spread in the res-
29 piratory tract. Here, we address the spread of viruses within epithelial tissue, using SARS-CoV-2
30 as a model pathogen. The overall considerations are similar for other viruses, but the param-
31 eters governing infection may vary considerably due to the specific countermeasures of the virus in
32 question, affecting its ability to bypass human antiviral defenses.

33 In terms of countermeasures, insufficient type I and III interferon secretion upon infection is a
34 main immune signature feature of SARS-CoV-2 infection (*Blanco-Melo et al., 2020; Hatton et al.,*
35 *2021; Stanifer et al., 2020; Minkoff and tenOever, 2023*). The failure to activate immediate antiviral
36 responses with IFNs is also a pathogenic aspect of other viruses including Ebola (*Mohamadzadeh*
37 *et al., 2007*), Marburg (*He et al., 2019*) and Herpes simplex (*Barreca and O'Hare, 2004*). Secretion
38 of IFN relies on the cell's ability to sense viral products during its replication. Despite the presence
39 of sensors for DNA and RNA viruses in cells, many species of viruses partially evade detection.
40 The SARS-CoV-2 virus is such a case: Only two of 16 putative RNA virus sensors, IFIH1 (MDA5) and
41 DHX58 (LGP2) from the RIG-I-like receptor (RLR) family, play roles in inducing IFN upon SARS-CoV-2
42 infection (*Yin et al., 2021*) and IFIH1 is antagonized by SARS-CoV-2 (*Liu et al., 2021*).

43 Intriguingly, evidence shows that pre-activated innate immune states help combat the SARS-
44 CoV-2 infection. The higher basal expression of viral sensors, IFIH1 and DDX58 (also from the RLR
45 family), in the upper airway of children (relative to adults), reduces the severity of COVID (**Loske**
46 **et al., 2022**). Furthermore, well-differentiated primary nasal epithelial cells derived from a donor
47 with pre-activated IFN γ do show resistance to SARS-CoV-2 infection (**Broadbent et al., 2022**). Thus,
48 the extent to which innate immunity contributes to the observed heterogeneity in responses to
49 SARS-CoV-2 between hosts (**Schaller et al., 2021; Desai et al., 2020**) is a compelling subject for
50 investigation.

51 To address this question, we reanalyze single-cell RNAseq data (**Fiege et al., 2021; Ravindra**
52 **et al., 2021**) providing gene expression profiles of virus sensors and antiviral genes in host cells dur-
53 ing early SARS-CoV-2 infection. We propose a cellular automaton model based on a few transition
54 rules suggested by observed cell states, to explain the heterogeneity in early disease progression
55 as a consequence of criticality in the virus-host interaction system.

56 Cell states during infection

57 Directly observing cell responses and cell state transitions in a patient's body upon viral infection
58 is virtually impossible. However, human bronchial epithelial cells (HBECs) mimic the airway epithe-
59 lium and have been used as a representative model for investigating the consequences of the viral
60 invasion (**de Jong et al., 1993, 1994; Davis et al., 2015**). Single-cell RNAseq provides snapshots of the
61 states of individual cells indicated by high-dimensional gene expression profiles at the mRNA level
62 and can uncover the heterogeneity of cell responses obscured by aggregate measurement. Thus,
63 by combining HBECs as a model and single-cell RNAseq data, one can in principle infer cell state
64 transitions following viral infection. More importantly, single-cell RNAseq also captures copies of
65 viral genes during sequencing, which allows us to simultaneously estimate viral replication inside
66 cells.

67 To reconstruct the trajectory of cell state transitions during early SARS-CoV-2 infection, we re-
68 analyze single-cell RNAseq data from experiments where HBECs are sampled before infection (0
69 h), as well as 24 and 48 hours post-viral infection (hpi) (**Fiege et al., 2021**). We focus on genes as-
70 sociated with antiviral responses and interferons from the host cells and detected viral genes. We
71 project high-dimensional gene expression data onto a 2D plane using Uniform Manifold Approx-
72 imation and Projection (UMAP) and obtain a low-dimensional visualization of single-cell expression
73 patterns (Fig. 1a). On the UMAP plane, each dot represents a cell sample and the distance between
74 dots correlates with the level of similarity of cellular states. The cells are not divided absolutely into
75 discrete clusters and rather show continuous trajectories. For simplicity and convenience, we clus-
76 ter the cells according to their gene expression.

77 Different clusters on the UMAP indicate distinct cellular states during the progression of infec-
78 tion. For instance, there are three sub-clusters of susceptible cells (O_1, O_2, O_3). Neither viral genes
79 nor IFNs are detected in these cells and only a few antiviral genes are expressed. The viral sensors
80 (DHX58, DDX58, and IFIH1) are at their lowest level (Fig. 1b, Fig. S1). We refer to all of these cells
81 as O cells due to their relatively similar gene expression profiles in terms of viral replication genes.
82 The proportion of O cells decreases over time as the infection spreads (Fig. 1c).

83 We also observe three infected cell clusters where viral genes are primarily detected, V^i , V^r ,
84 and V . With the increasing counts of viral genes, we infer that the V^i cluster is the earliest state
85 after an O cell has been infected and the virus begins to replicate. Some but not all antiviral genes
86 are activated in the V^i cells (IFIT1/2/3 and OAS1/2/3) (Fig. 1b and Fig. S1), indicating that these cells
87 are still vulnerable to viral invasion. This cluster is followed by two subsequent clusters, the V^r
88 cluster with pronounced viral replication and A cluster with barely any viral replication.

89 In the V cluster, the viral genes reach their highest level and antiviral genes are strongly inhib-
90 ited, indicating that the virus has fully hijacked the cell. The antiviral genes are expressed most
91 strongly in the A cluster and partially in the N cluster, indicating that the antiviral capability of the

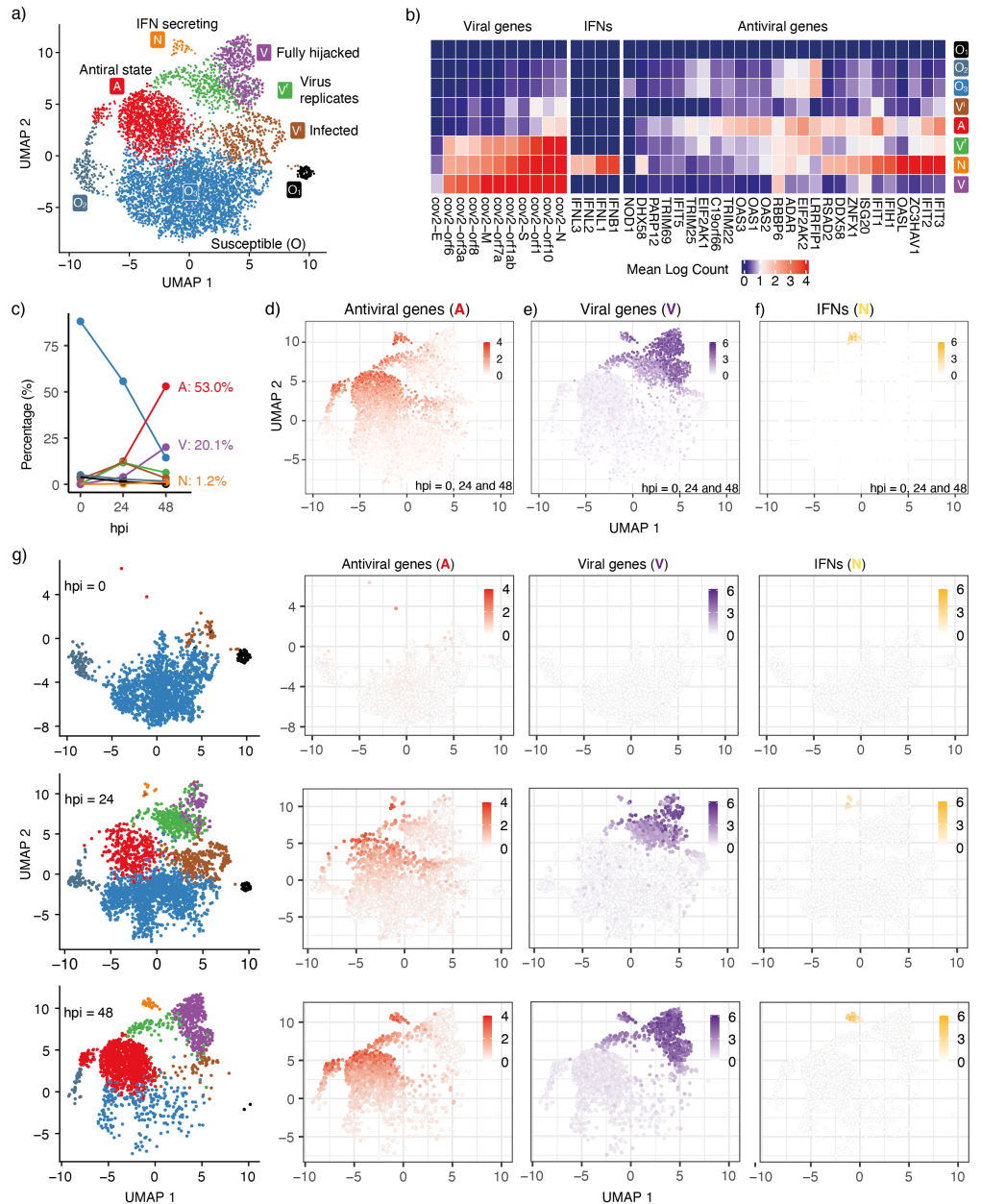


Figure 1. Cell states during SARS-CoV-2 infection in human tracheal/bronchial epithelial cells. **a)** 6162 cells (Fiege *et al.*, 2021) covering samples of mock-infected (0 h), 24 hpi (hours post-infection), and 48 hpi visualized with UMAP. **b)** Average expression of representative viral genes, IFNs, and antiviral genes with each cell cluster (state). **c)** Cell proportions of clusters at different time points (hpi = 0, 24, and 48). Cell proportions are labeled with corresponding colors in **a)**. **d)** Average expression (0–48h) of antiviral genes (IFIT1, IFIT2, IFIT3, IFIT5, IFIH1, OAS1, OAS2, OAS3, OASL, DDX58). **e)** Average expression (0–48h) of viral genes (cov.orf1ab, cov.S, cov.orf3a, cov.orf6, cov.M, cov.N). **f)** Average expression (0–48h) of interferon genes (IFNB1, IFNL1, IFNL2, IFNL3). 103 cells (1.7%) are IFN-positive. **g)** Progression of viral infection as indicated by changes in cell proportions of different states. Cells are shown separately at each time point in the leftmost column. The right columns show the average expression of antiviral genes, viral genes, and IFNs in the corresponding cells.

92 *N* cluster is weaker than the full antiviral state. Although the *N* cluster also shows a high level of
 93 viral genes, it severely lacks one of the viral genes (cov.E, Fig. S2) compared with the most highly
 94 expressed viral genes of the *V* cluster. This observation implies that viral replication and activa-
 95 tion of the antiviral state coexist in the IFN-secreting cells (*N* cluster). We note the existence of a

96 small subgroup of the V^r cluster, close to the A cluster, that exhibits relatively high levels of both
97 antiviral genes and viral genes but no appreciable IFN (Fig. 1d–f). The viral genes are also partially
98 expressed in these cells, but different from the N cluster, the antiviral genes are fully expressed
99 (Fig. S1 and S2). Thus, these cells are more likely to sustain the antiviral state.

100 At 24 hpi, some cells have switched from the pre-infection state (O) to other states. At 48 hpi,
101 almost all cells have transitioned to other states and only a few cells remain in the O state (Fig.
102 1c and g). The aggregated gene expression of representative antiviral genes and detected viral
103 genes indicates the cells move from the O state towards the three remaining terminal states on
104 the considered timescale of 2 days: Antiviral state (A , Fig. 1d), Virus-conquered state (V , Fig. 1e),
105 and IFN producing state (N , Fig. 1f). Central for the overall defense is the relatively few cells that
106 reach the IFN-producing state (N). These cells also express A and V genes.

107 When IFN is not expressed, the antiviral genes and viral genes exclude each other (Fig. 1d and
108 e), except for a few cells around (UMAP1, UMAP2) $\sim (-2.5, 7.5)$ (green cells at hpi = 48, Fig. 1g). They
109 represent cells where the virus succeeded in stopping IFN secretion, but could not fully hijack the
110 cell. We still regard these cells as antiviral cells in our model.

111 The N state is associated with both high levels of virus sensors and viral genes, in agreement
112 with the observation that IFN production is initiated after exposure to the virus (*Lei et al., 2020*)
113 and that IFN can induce an antiviral state inside the same cell (*Sanceau et al., 1987*). Expression
114 of the key SARS-CoV-2 sensitive sensors (IFIH1, DDX58, DHX58) is sparse in the O state (Fig. S1),
115 indicating that a small fraction of cells have virus-sensing capacity prior to infection and are ready
116 to mount a defense – and that this population increases with IFN tissue diffusion.

117 Model

118 We introduce a cellular automaton model to capture the cell state dynamics during early stages of
119 SARS-CoV-2 infection in a sheet of epithelial tissue. At each simulation, we seed an infection site on
120 a 2D square lattice and study how the infection spreads as the sites on the lattice switch between
121 cell states following a set of simple rules derived from the observations of the single-cell RNAseq
122 data.

123 In addition to the states corresponding to the dominant clusters observed in the single-cell
124 data (Fig. 1a) (O , A , V and N states corresponding to O , A , V and N clusters), we introduce a
125 transient pre-antiviral state (a) that can switch to the N state rapidly on viral exposure, considering
126 the heterogeneity of viral sensing ability in susceptible cells.

127 It follows from this description, that those RNA viruses that can sensed by a large repertoire of
128 sensors should be modeled with a larger fraction of cells in the a state.

129 The model is initialized with cells predominantly in the O state and a small fraction, p_a , in the
130 pre-antiviral state a . The parameter p_a can also be understood as the probability that an O cell will
131 switch to the N or A state when exposed to the virus or IFNs, respectively. As such, the value of p_a
132 depends on both host and virus. In particular, a virus that is able to effectively interfere with the
133 defense and signaling of host cells will be modeled by a low p_a value.

134 It is worth noting that the proportion of cells in the a state before the onset of SARS-CoV-2
135 infection is expected to be higher in hosts with pre-activated antiviral innate immunity (*Loske et al.,*
136 *2022; Broadbent et al., 2022*), meaning that the value of p_a will, in general, depend on the exposure
137 history of the host.

138 We propose the following transitions between five main discrete cell states (Fig. 2a):

- 139 • N , IFN-secreting cells. These arise from pre-antiviral cells (a state) that become infected (but
140 not infectious). Here we ignore possible apoptosis (*Wen et al., 1997; Tesfagizi, 2006*) of N
141 cells since IFNs still have time to diffuse to the neighborhood.
- 142 • O , unaffected (susceptible) cells.
- 143 • V , infected cells, virus-producing cells. This state arises when a susceptible (O) cell is exposed
144 to a virus from another V cell.

- 145 • a , pre-antiviral state. May develop into either the A or N state upon exposure to signals from
- 146 N cells or virus from V cells.
- 147 • A , antiviral state. Immune to infection. Achieved when a pre-antiviral (a) cell is exposed to IFN.
- 148 We do not consider the decay of the antiviral state as it may last more than 72 h (*Gajetaan*
- 149 *et al., 2013*).

150 The dynamics are defined in terms of discrete time steps, representing the characteristic timescales
 151 of cellular viral infection. We explore the model for an extended time, keeping in mind that in reality
 152 other immune cells such as NK-killer cells and macrophages may migrate to the infected site and
 153 reduce viral spread (*McNab et al., 2015*).

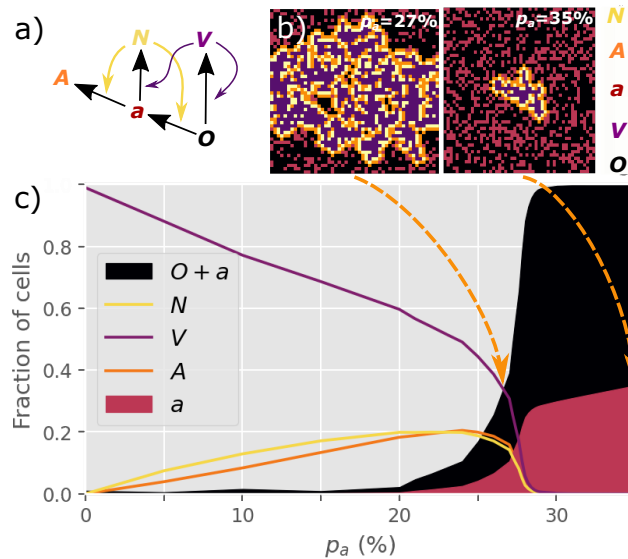


Figure 2. NOVAa model. **a)** The cell state transitions are included in the NOVAa model. The simpler OVA model bypasses the a and N states, by allowing V to induce direct $O \rightarrow A$ transitions (Fig. S3). **b)** Final states of a small lattice (50×50) simulations at two different values of p_a (both at IFN spreading radius $R = 1$). **c)** The fraction of cells in each state in the final frozen configuration as a function of p_a . A critical transition is observed at $p_a = p_c \sim 27.8\%$. At lower values of p_a , most cells terminate in the V state, representing an aggressive tissue infection. Simulations were performed on a lattice with linear dimension $L = 1000$.

154 The four rules of the model are (Fig. 2a):

$$155 \quad N(a) = A, \quad N(O) = a, \quad V(a) = N, \quad V(O) = V$$

156 where the notation $X(Y) = Z$ denotes a cell in state X acting on a cell in state Y and changing it to
 157 state Z in one time-step. Thus, cells in states O , a , and A are unable to influence their neighbors.
 158 The V state is the only directly self-replicating state.

159 Each site of the $L \times L$ lattice is assigned to either the O (probability: $1 - p_a$) or the a state (prob-
 160 ability: p_a). Infection is initiated by a single V cell, and we explore the percolation of the infection
 161 to larger scales. A time step consists of L^2 updates, in which a random site i is selected. If a V cell
 162 is selected, it interacts with its 4 nearest neighbors according to the rules $V(O) = V$ and $V(a) = N$.
 163 If an N cell is selected, it interacts with all cells within a radius R , according to the rules $N(O) = a$
 164 and $N(a) = A$. The radius R thus quantifies the diffusion range of IFNs relative to the virus.

165 Results

166 At $R = 1$, the final number of infected cells depends strongly on the value of p_a . At a low p_a of 0.27,
 167 infections typically spread to the entire system, while at a higher p_a of 0.35, the propagation of the
 168 V state is inhibited (Fig. 2b).

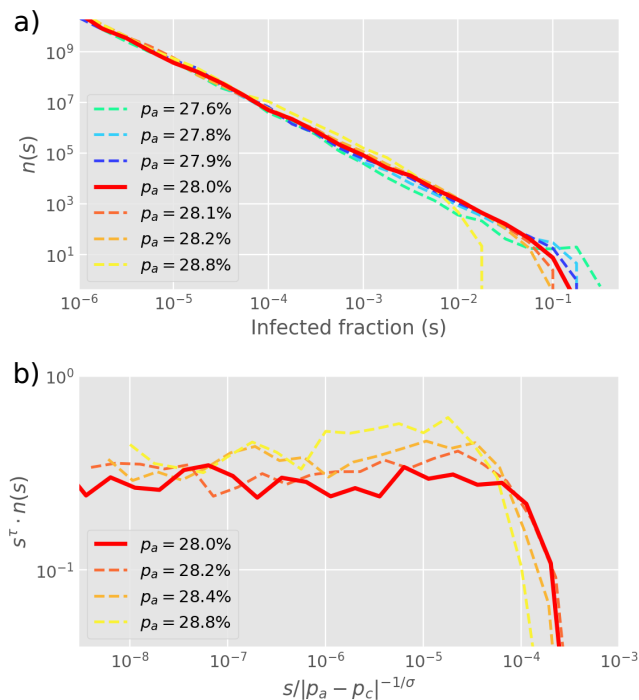


Figure 3. Cluster size distribution. **a)** The distribution of infected cells ($s = (N + V)/L^2$) for different values of p_a , simulated by starting with one infected cell in a 2D square lattice of linear extent $L = 2000$. **b)** The exponents from a) are extracted by re-scaling as shown on the y-axis, yielding $\tau = 1.83$. The cut-off exponent is estimated as $\sigma \sim 1$. Simulations plot the final outbreak sizes from 10,000 initial infections of one cell. The histogram is log-binned with 5 bins per decade. The critical point at $p_a = p_c = 0.28$ is determined as the value with the longest scaling regime.

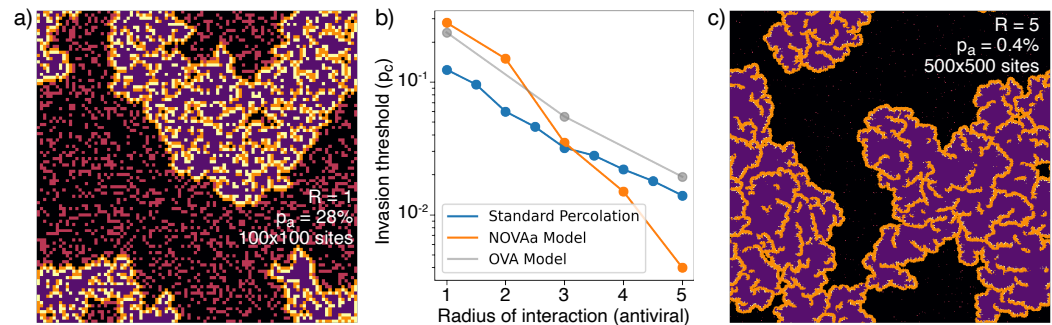


Figure 4. Range of IFN. **a)** Typical cluster for an $R = 1$ simulation at $p_a \sim p_c = 0.278$. **b)** The dependence of p_c with R , approximately reproduced by a fit $p_c \sim 3^{-R}$. For comparison the OVA model as well as percolation has $p_c \sim 3^{-R/2}$. In all cases, when p_a is above p_c then the virus is prevented from spreading. **c)** Cluster distribution for $R = 5$ at $p_a \sim p_c = 0.004$, at a 5 times larger linear scale than a).

169 We observe a threshold-like behavior of the final attack rate of the virus when the initial p_a
 170 changes continuously (Fig 2c). The virus spreads macroscopically for $p_a < p_c \approx 27.8\%$. At higher p_a ,
 171 cells are sufficiently prone to convert to the antiviral state to prevent the infection from percolating.
 172 The size distribution $P(s)$ of infection clusters around the critical value of $p_a = 27.8\%$ obeys
 173 power-law decay (Fig. 3a). In Fig. 3b, the distribution $P(s) \propto 1/s^\tau$ is further explored by re-scaling
 174 and the cluster size exponent is confirmed as $\tau = 1.83 \pm 0.03$ when $p_a = 28\%$. Notably, this exponent
 175 is below the equilibrium 2D percolation yielding $\tau = 2.05$ (Stauffer and Aharony, 2018). Further,
 176 our exponent $\tau \sim 1.8$ is above to the percolation-inspired cluster growth model for virus spread of
 177 ref. (Gönci et al., 2010) which has an exponent between $\tau = 1.58$ and $\tau = 1.64$ depending on the

178 distribution of individual cells' pre-defined ability to become infected.

179 The actual critical value of p_a depends strongly on the choice of neighborhood. In particular, at
180 $R = 1$, the V and N states have the same range in the tissue (a proxy for diffusivity), while a more
181 realistic scenario is to allow IFNs to diffuse faster in the tissue ($R > 1$), facilitating the initiation of
182 the antiviral state. The critical percolation threshold p_c decreases almost exponentially with the
183 value of R (Fig. 4b), and viral propagation can be stopped for p_a as low as 0.4% when $R \geq 5$. Such a
184 small fraction of initial cells in the a state is consistent with the remarkably few N cells observed in
185 experiments (Fig. 1b). Thus, a higher diffusivity of IFN provides a more than proportional decrease
186 in the required number of antiviral cells. As revealed by the reanalysis of RNAseq data in Fig. 1, the
187 fraction of IFN-positive cells is relatively low – around 1.7%. Comparing with simulations near the
188 critical point, we find that, at $R = 5$, the ratio of N cells to all affected cells ($N + A + V$) in the final
189 state, $\lim_{t \rightarrow \infty} N / (N + A + V) \approx 2\%$, i.e. it is of comparable magnitude to the experimental value. This
190 holds in a wide range around the critical point, $p_a \sim p_c$.

191 The exponents for the cluster size distribution are the same at $R = 1$ and $R = 5$, while the
192 structures of the clusters are different (Fig. 4a and c). Greater R leads to a different microscopic
193 structure with fewer A and N cells in the final state (Fig. 4c).

194 To put the above findings in perspective we further explore a simplified version of our model
195 with only 3 states (supplementary Fig. S3), the OVA model, which may be seen as a rephrasing of
196 models for induced antiviral states suggested by *Howat et al. (2006)*; *Segredo-Otero and Sanjuán*
197 *(2020)*; *Michael Lavigne et al. (2021)*. In the OVA model, p_a is the probability that an infected cell
198 produces interferons to warn neighbor cells within radius R . In the OVA model, one update consists
199 of selecting a random cell. If the cell is in the V state then its neighbor cells may change by exposure
200 to the virus, provided that they are susceptible (O). Each of the four neighbors is now chosen in
201 random order, and if a neighbor cell i is in the O state, a random number $ran_i \in [0, 1]$ is drawn. If
202 $ran_i \geq p_a$ the neighbor is flipped to the V state. If, on the other hand, $ran_i < p_a$, all O cells within a
203 radius R around the neighbor i are converted to the A state. Thus, for large R and moderate p_a , the
204 spread of infection will be mitigated. We find that the OVA model has an "outbreak size" exponent
205 $\tau \sim 1.8$, similar to the NOVAa model. However, the change in microstructure as a function of the IFN
206 range R observed in the NOVAa model (compare Fig. 4 panel a and c) is not observed in the OVA
207 model (Fig. S3), where the features instead scale proportionally with R . We also simulated standard
208 percolation by randomly adding disks of radius R of blocking ("antiviral") cells and checking for
209 percolation of the infected state. While the critical behavior of the standard percolation model
210 approximately resembles that of the OVA model (Fig. 4b), the antiviral state of the OVA model is
211 somewhat less effective at blocking the spread (reflected in a higher threshold p_c).

212 Finally, we examined a version of the model where the discrete idealization of N -cells acting
213 at all cells within a specific radius R is replaced by a probabilistic conversion with a diffusion-like
214 profile. The algorithm for this is described in the supplement, with results in Fig. S4 to be compared
215 to Fig. 4. We find that the probabilistic spreading of IFN is more effective, in terms of demanding
216 lower R for obtaining similar limits on spreading of the infection.

217 Discussion

218 There are some preexisting models of the interplay between virus, host cells and triggered immune
219 responses, with an antiviral state triggered by IFN signaling from neighbor cells (*Graw and Perel-*
220 *son, 2016*). Cellular automaton models of infection dynamics in epithelial tissue were explored
221 by (*Howat et al., 2006*; *Segredo-Otero and Sanjuán, 2020*; *Michael Lavigne et al., 2021*), with the
222 overall result that spreading depends on competition between the virus and an induced antiviral
223 cell state. This competition is recapitulated in our model in terms of the two effective parameters
224 p_a and R . Our model emphasizes the threshold dynamics, with a critical transition between effec-
225 tive confinement and unhindered spread that depends sensitively on the details of the relevant
226 cell states. In particular, the presence of the specialized IFN-producing N cells allows for disease
227 confinement at a much lower concentration of pre-antiviral cells (lower value of p_a) in the NOVAa

228 model, than in the OVA model which lacks the N state (Fig. 4b). As a consequence of low p_a , the
229 number of final N -state cells is also much lower.

230 The low concentration of ready-to-fight cells may seem perplexing, leading one to surmise that
231 the organism could easily fight off an infection by only slightly increasing its investment in these
232 primed cells. However, one should keep in mind that e.g. the human organism does indeed have
233 ready-to-fight cells that are able to eliminate most foreign RNA, and only leave a few truly infectious
234 viruses. As highlighted in the introduction, these select viruses often employ strategies to lower
235 the p_a , for example by only being sensed by a small fraction of the RNA virus-sensitive receptors of
236 our cells.

237 The parameter p_a can be interpreted as the probability that a cell is sufficiently antiviral to con-
238 vert to a N state upon infection with a given virus. The relevant value of p_a will depend on the virus
239 considered (and will be small for viruses that inhibit cell responses to infection) as well as on the
240 host (e.g. on age (*Kissler et al., 2020*) and recent infection history). Dysregulated IFN responses
241 are characteristic of the effective immunomodulatory strategies used by betacoronaviruses (*Chan-*
242 *nappanavar et al., 2019; Acharya et al., 2020*).

243 The parameter R reflects the signaling efficiency of an interferon-producing cell. Since R is mea-
244 sured in units of the typical distance that the virus spreads, it depends on viral properties, including
245 its burst size, diffusion, and adsorption to host cells, with higher adsorption being associated with
246 larger R values. For SARS-CoV-2 this suggests that lower ACE2 receptor counts would result in less
247 adsorption to nearby cells, in turn allowing the virus to spread to more distant tissues (*Bastolla,*
248 *2021*) suggesting a lower value of R .

249 For viruses that do not delay the production of IFNs, p_a would be higher than for SARS-CoV-2,
250 allowing neighbor cells around an infected site to form a kind of “ring vaccination” as the antiviral
251 state dominates. In this sense, our model is consistent with the previous modeling of the roles of
252 autocrine and paracrine interferon signaling suppression of viral infection (see e.g. (*Michael Lavi-*
253 *gne et al., 2021*) for parallels between IFN response and ‘ring vaccination’).

254 We do not consider viral particles which enter the bloodstream and seed new infections non-
255 locally. This may allow the virus to spread in the tissue at what would otherwise constitute sub-
256 critical conditions in our model. Further, there may be tissue-specific variations in both p_a and R ,
257 adding larger-scale heterogeneity to the overall spreading. As the disease progresses one would
258 expect additional heterogeneity to emerge, associated with variability in later host responses in-
259 cluding macrophage activation and adaptive immunity (*Wang et al., 2021*).

260 The remarkable heterogeneity of disease progression in COVID-19, in the form of widely vari-
261 able symptoms (*Tabata et al., 2020*) and transmission risk (*Nielsen et al., 2021; Kirkegaard and*
262 *Sneppen, 2021*), has been widely observed. E.g. among university students, just 2% of SARS-CoV-2
263 positive hosts provided 90% of total respiratory viral load (*Yang et al., 2021*). In our formalism,
264 we would understand such variability in terms of a p_a that is comparable to the critical value, but
265 varying between hosts. A slight change of p_a then results in dramatic fluctuations in the outcome
266 of an infection.

267 To be more quantitative, for SARS-CoV-2 the detected virus count on average grows by a factor
268 of 3.5 (*Kissler et al., 2020*) in one infection generation of 8 hours (not to be confused with the
269 between-host ‘generation time’ of the infection). This within-host reproductive number is far below
270 the number of viruses produced from a cell, indicating severe restrictions from the innate immune
271 system. On the other hand, 3.5 is still above the threshold for spreading, indicating that within-host
272 amplification is super-critical. However, the measured amplification includes viruses that “jump” to
273 other spots in an infected person, thereby suggesting a local spreading that is closer to the critical
274 value than an amplification of 3.5 would suggest.

275 Our study finally compared the NOVAa model with the simpler OVA scenario that recapitulates
276 earlier modeling of induced antiviral states (*Howat et al., 2006; Segredo-Otero and Sanjuán, 2020;*
277 *Michael Lavigne et al., 2021*). These papers all build on a more homogeneous role of infected
278 cells, each inducing some immunization of surrounding cells. Ref. (*Howat et al., 2006*) emphasizes

279 the larger range of IFN signals compared to viral diffusion, while the focus of (*Segredo-Otero and*
280 *Sanjuán, 2020*) is competition between viruses with different abilities to suppress IFN signaling.
281 Ref. (*Michael Lavigne et al., 2021*) introduces a cellular automaton approach where the antiviral
282 state leads to a type of ring vaccination that prevents the virus from spreading when more IFN is
283 produced. Our OVA model may be seen as a simplified and more stochastic version of this last
284 model. The NOVAa model then adds the additional benefits associated with the experimentally
285 observed but low-abundance *N* state cells, which by their rarity adds to predicted randomness
286 between the fate of individual infection centers during an early viral infection.

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