1 Time series analysis of daily data of COVID-19 reported cases in Japan from

2 January 2020 to February 2023

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NOTE: This preprint reports new research that has not been certified by peer review and should not be used to guide clinical practice.

10 Abstract

11 This study investigated temporal variational structures of the COVID-19 12 pandemic in Japan using a time series analysis incorporating maximum entropy method (MEM) spectral analysis, which produces power spectral densities (PSDs). This method 13 14 was applied to daily data of COVID-19 cases in Japan from January 2020 to February 15 2023. The analyses confirmed that the PSDs for data in both the pre- and post-Tokyo Olympics periods show exponential characteristics, which are universally observed in 16 17 PSDs for time series generated from nonlinear dynamical systems, including the so-called 18 susceptible/exposed/infectious/recovered (SEIR) model, well-established as а mathematical model of temporal variational structures of infectious disease outbreaks. 19 20 The magnitude of the gradient of exponential PSD for the pre-Olympics period was 21 smaller than that of the post-Olympics period, because of the relatively high complex 22 variations of the data in the pre-Olympics period caused by a deterministic, nonlinear 23 dynamical system and/or undeterministic noise. A 3-dimensional spectral array obtained 24 by segment time series analysis indicates that temporal changes in the periodic structures 25 of the COVID-19 data are already observable before the commencement of the Tokyo 26 Olympics and immediately after the introduction of mass and workplace vaccination 27 programs. Lessons from theoretical studies for measles control programs may be 28 applicable to COVID-19.

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30 Introduction

Since December 2019, a novel coronavirus designated as Severe Acute
 Respiratory Syndrome Coronavirus 2 (SARS-CoV-2) has rapidly spread around the world,

33	affecting millions of people worldwide; its impact continues today. Waves of cases of
34	this novel coronavirus disease, also known as COVID-19, still occur recursively, although
35	these waves may well be prevented, and possibly eradicated, in the future. Considerable
36	effort to prevent and eradicate COVID-19 has been expended through COVID-19
37	surveillance, vaccinations, and theoretical and experimental research [1-4]. Among these
38	efforts, attempts to elucidate the mechanism of the COVID-19 pandemic have been of
39	great interest. Recently, researchers have tried to interpret the behavior of the pandemic
40	in terms of deterministic chaos [5-7]. Sapkota et al., reported that the hosting of the Tokyo
41	Olympic Games in Japan between 23 July and 8 August 2021 affected the mechanism of
42	the COVID-19 pandemic in the country [8]. Therefore, the temporal variational structures
43	of the data before and after the Olympic Games may differ, and examining this point is
44	significant from the standpoint of predicting the COVID-19 pandemic. However, typical
45	approaches cannot fully elucidate the temporal variational structures of the patterns of the
46	pandemic. This is because the data lengths of reported cases of COVID-19 are very short:
47	in Japan, the data are collected daily, and the number of data points was slightly above
48	1000 points by February 2023. Thus, a superior and powerful method of time series
49	analysis to elucidate the temporal variational structure of time series of even short data
50	length is required. In previous publications [9-11], we proposed a method that enables us

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51	to analyze the time series of COVID-19 cases. In the present study, this method was
52	applied to examining the temporal variational structures of daily time series data of
53	reported COVID-19 cases for the entire country of Japan. Quantitative elucidations of the
54	COVID-19 pandemic are of great significance in epidemiology, and will contribute to the
55	development of surveillance of the disease.
56	
57	Methods
58	Data
59	The present study analyzed daily data of reported COVID-19 cases for the entire
60	country of Japan from 16 January 2020 to 21 February 2023 (1133 data points). During
61	this period, a total 32,851,731 cases of COVID-19 were reported in Japan. The data used
62	in the present study were obtained from the Japan Ministry of Health, Labour, and
63	Welfare COVID-19 Data [12]. The data are indicated in S1 Dataset.
64	
65	Time series analysis
66	We used a time series analysis consisting of maximum entropy method (MEM)
67	spectral analysis in the frequency domain and least squares method (LSM) in the time
68	domain [9-11,13,14]. The MEM is considered to have a high degree of resolution of
69	spectral estimates compared with other analysis methods of infectious disease

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70	surveillance data such as the fast Fourier transform algorithm and autoregressive methods,
71	which require time series of long data lengths [15, 16]; therefore, an MEM spectral
72	analysis allows us to precisely determine short data sequences, such as the infectious
73	disease surveillance data used in this study [9-11,13-15].

74

75 MEM spectral analysis

We assumed that the time series data x(t) (where t is time) were composed of

77 systematic and fluctuating parts [17]:

78
$$x(t) =$$
systematic part+fluctuating part. (1)

To investigate temporal patterns of x(t) in the monthly time series data, we performed MEM spectral analysis [9-11,13,14]. MEM spectral analysis produces a power spectral density (PSD), from which we obtain the power representing the amount of amplitude of x(t) at each frequency (note the reciprocal relationship between the scales of frequency and period). The MEM-PSD, P(f) (where *f* represents frequency), for the time series

84 with equal sampling interval Δt , can be expressed by

85
$$P(f) = \frac{P_m \Delta t}{\left|1 + \sum_{k=-m}^{m} \gamma_{m,k} \exp\left[-i2\pi f k \Delta t\right]\right|^2},$$
 (2)

86 where the value of P_m is the output power of a prediction-error filter of order m and $\gamma_{m,k}$

is the corresponding filter order. The value of the MEM-estimated period of the *n*th peak component T_n (=1/ f_n ; where f_n is the frequency of the *n*th peak component) can be determined by the positions of the peaks in the MEM-PSD.

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91 Least squares method

The validity of the MEM spectral analysis results was confirmed by calculating the least squares fitting (LSF) curve pertaining to the original time series data x(t) with MEM-estimated periods. The formula used to generate the LSF curve for X(t) was as follows:

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$$X(t) = A_0 + \sum_{n=1}^{N} A_n \cos\{2\pi f_n(t+\theta_n)\}.$$
 (3)

97 The above formula is calculated using the LSM for x(t) with unknown parameters f_n , A_0 98 and A_n (n = 1, 2, 3, ..., N), where f_n (= $1/T_n$; T_n is the period) is the frequency of the *n*-th component; A_0 is a constant that indicates the average value of the time series data; A_n is 99 100 the amplitude of the *n*-th component; θ_n is the phase of the *n*-th component; and N is the 101 total number of components. The reproducibility level of x(t) by the optimum LSF curve 102 was evaluated via a Spearman's rank correlation (p) analysis performed using SPSS 103 (Statistical Package for the Social Sciences) version 17.0J software (SPSS, Tokyo, Japan). 104A *p* value of ≤ 0.05 was considered statistically significant.

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106 **Results**

107 Temporal Variations in COVID-19 Reported Cases Data

Daily data of reported cases of COVID-19 from 16 January 2020 to 21 February 2023 in Japan are plotted in Fig 1a. A closer view of the data from January 2020 to June 2021 is illustrated in Fig 1b, which shows four large waves observed at intervals of about four to five months, peaking in April and July 2020, and January and May 2021. Subsequently, Fig 1a shows four large waves at longer intervals than before, approximately five to six months, with peaks in August 2021, February and August 2022, and January 2023.

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116 Fig 1. Daily data of COVID-19 reported cases of Japan from 16 January 2020 to 21

February 2023. (a) The original data. (a') Histogram of the original data. (b) Enlargement of the original data from 16 January 2020 to 30 June 2023. (c) The logarithm-transformed data of the original data (thin line) and its optimum LSF curve (bold line). (d) MEM-PSD of the residual data in the low-frequency range ($f \le 1.2$). (e) The residual data obtained by subtracting the LSF curve from the log-data. (e') Histogram of the residual data. Small vertical line in *e* indicates the boundary of phase I (pre-Tokyo Olympic Games, 11 February 2020–22 July 2021) and phase II (post-Tokyo Olympic

124 Games, 23 July 2021–21 February 2023).

125

126 **Preparing the data for analysis**

127 We take the reported cases data x(t) (t: time) to represent discrete ones at $t = k\Delta t$ (k = 128 1, 2, 3, $\cdots N$) where Δt is the time interval and N the length of the time series ($\Delta t = 1$ -day 129 and N = 1133, in the present study). Fig 1a' gives the frequency histogram for x(t) (Fig 130 1a). This histogram is apart from the normal distribution required for conventional 131 spectral analysis. Then, we introduced the logarithm transformation of x(t) (Fig 1a). 132 Because the data from 16 January to 10 February 2020 include 17 zero values and are not 133 available for the logarithm transformation, the 15 cases that were reported during this period are ignored and the starting point of the data was re-set to 11 February 2020. As a 134 135 result, the present study uses the data from 11 February 2020 to 21 February 2023. For 136 the data in this period, the logarithm-transformed data is shown in Fig 1c, where the 137 spikiness of the reported cases observed in x(t) has been reduced, and a long-term 138 decreasing trend is observed.

To remove the long-term trend of the log-data shown in Fig 1c, PSD, P(f) (*f*: 140 frequency), for the log-data was calculated, and the PSD ($f \le 1.2$) is displayed in Fig 1d 141 (unit of *f*: 1/year). Therein, the longest period can be observed as the prominent peak at

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142	the position of 5.3-year period. With this 5.3-year period, we modeled the long-term trend
143	in the COVID-19 pandemic by calculating the LSF curve (Equation (3)) for the entire
144	log-data (Fig 1c). The LSF curve obtained (Fig 1c) expresses the long-term trend of the
145	log-data well.
146	We removed the LSF curve from the log-data (Fig 1c), and the residual time series
147	data were obtained, as shown in Fig 1e. The frequency histogram for this residual data is
148	shown in Fig 1e' and approximates to the normal distribution required for conventional
149	spectral analysis. Normality of distribution was assessed using the χ^2 fitting test, and the
150	null hypothesis was not rejected ($P = 0.76$).
151	
152	Power spectral density of the time series data
153	To investigate the effect of hosting the Tokyo Olympic Games on the temporal
154	variational structures of the COVID-19 pandemic in Japan, the residual data (Fig 1e) were

155 divided into two ranges (phases I and II) in accordance with the starting and ending points

156 of the Tokyo Olympic Games (23 July 2021 and 8 August 2021, respectively): pre-

157 Olympic Games (11 February 2020 – 22 July 2021) for phase I and post-Olympic Games

158 (23 July 2021 - 21 February 2023) for phase II. MEM-PSDs for the residual data of

159 phases I and II were calculated. The semi-log plots of the PSD are shown in Fig 2a and

160	2b for phases	I and II,	respectively.
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162	Fig 2. MEM-PSDs for two ranges of the residual data ($f < 30.0$). (a) Phase I (pre-
163	Tokyo Olympic Games, 11 February 2020–22 July 2021). (b) Phase II (post-Tokyo
164	Olympic Games, 23 July 2021- 21 February 2023).
165	
166	Gradient of power spectral density
167	As seen in the PSDs for phases I and II in Figs 2a and 2b, respectively, the overall
168	trend of each PSD indicates the exponential form
169	$P(f): \exp(-\lambda f) \tag{4}$
170	until the PSDs level off at the lowest limit determined by the accuracy of the present data,
171	that is, the number of significant digits in the data. The values of λ for phases I and II are
172	0.25 and 0.28, respectively.
173	
174	Dominant spectral lines
175	Close-ups of the low-frequency regions of the PSDs in Figs 2a and 2b are shown
176	in Figs 3a and 3b, respectively. For phase I (Fig 3a), the dominant spectral peak is
177	observed at $f = 2.8$, corresponding to a 0.36-year (4.3-month), with considerably large

178 powers representing the amplitude of x(t) at each frequency. For phase II (Fig 3b), the

179	dominant spectra	peak is observed	d at f =	= 2.0, corr	esponding t	o a 0.50-year	(6.0-month),
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- 180 with considerably large powers.
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Fig 3. Close-up of the low-frequency region (f < 4.0) in Figs 2a and 2b: (a) Phase I</li>
(pre-Tokyo Olympic Games, 11 February 2020–22 July 2021). (b) Phase II (post-
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184 Tokyo Olympic Games, 23 July 2021–21 February 2023).

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186 Segment time series analysis

187 Periodic structures of the residual data were further investigated via segment 188 time series analysis (Fig 1e). The residual data (Fig 1e) are divided into multiple segments, 189 and the PSD is calculated for each segment. In this study, each segment represents the 190 time interval of 365 days, and the starting point of two consecutive segments is delayed by six days. The PSDs thus obtained are shown as a 3D spectral array in Fig 4. In the 3D 191 192 spectral array, the power is plotted against the frequency (horizontal axis) and time (right 193 vertical axis). In the frequency range of 1.0 < f < 4.0, corresponding to the periods of 3.0 194 months to 1 year, spectral lines are clearly observed over the whole time range. 195 The temporal variations of the frequency of dominant spectral lines observed in 196 the 3D spectral array (Fig 4) are plotted in Fig 5. As seen in the figure, spectral peaks

197	were observed around $f = 3.0$ (0.33 year) before May 2021. After May 2021, and
198	beginning before the Tokyo Olympic Games started in July 2021, spectral peaks
199	gradually migrated to the low-frequency range, and were observed to be around $f = 2.2$
200	from July to November 2021, and then remained relatively constant around $f = 2.0$
201	thereafter.
202	
203	Fig 4. Three-dimensional spectral array for the residual data in the frequency range
204	of $1.0 \le f \le 10.0$.
205	
206	Fig 5. Temporal variations of the frequencies of dominant spectral peaks detected
207	in the frequency range of $1.0 \le f \le 4.0$.
208	
209	Discussion
210	The most notable result obtained in the present study is that, as observed in Fig
211	5, the gradual migration of the spectral line to the low-frequency range from 3.0 (0.33-
212	year) to 2.0 (0.5-year) during May to July 2021 is already observable before the
213	commencement of the Tokyo Olympic Games in July 2021 and immediately after the
214	introduction of mass and workplace vaccination programs in April 2021, at a time when
215	Japan's vaccination rate was 4%. The vaccine rate increased quickly from May; the

216	maximum number of daily inoculations was 1.6 million. By October 2021, more than 77
217	million people, equivalent to 61.8% of the targeted population, had completed the
218	vaccination series [18]. The temporal behavior of periodic structures observed in Fig 5
219	indicates that theoretical studies for measles control programs, based on predictions that
220	vaccination generates an increase in the inter-epidemic period (IEP), corresponding to the
221	interval between major waves of an epidemic, may also apply to COVID-19 [19,20]. The
222	IEP of measles epidemics has been investigated with time series analysis and
223	mathematical models [21-27]. The IEP represents the amount of time required to
224	accumulate a cohort of susceptible individuals that is sufficiently large to allow the
225	measles virus to effectively spread over a community once it is introduced from outside.
226	Our previous work investigated the IEP of measles epidemics in Japan and Wuhan in
227	China using the present method of spectral analysis [19,20], and confirmed that the IEP
228	increases as the vaccination ratio increases, as predicted by theoretical studies for a
229	mathematical model of temporal variational structures of infectious diseases [21,22,28].
230	Based on the theoretical studies of measles and our preceding work in that disease, the
231	present finding that period structures of the COVID-19 data of Japan changed temporally
232	after May 2021 may be the effect of the increased vaccination rate in the previous month,
233	April 2021.

234	With respect to the exponential characteristics of the PSDs for COVID-19 data
235	(Figs 2a and 2b), our preceding work clarified that the PSDs for the time series generated
236	from deterministic, nonlinear dynamical systems, such as the so-called
237	susceptible/exposed/infectious/recovered (SEIR) epidemic model [29] and the Rössler,
238	Lorenz and Duffing models [30,31], exhibit exponential characteristics. With respect to
239	infectious disease epidemics, preceding research has confirmed that exponential spectral
240	peaks are observed for incidence data of measles in Japan [15], Wuhan [19], New York
241	City [29] and several communities in Denmark, the UK and the USA [32], as well as for
242	chaotic and periodic time series generated by the SEIR epidemic model [29]. Thus, the
243	present finding of exponential characteristics of the PSDs for COVID-19 (Figs 2a and 2b)
244	suggests that the number of reported cases of COVID-19 in Japan is based on
245	deterministic nonlinear dynamics.

For the magnitude of the PSD gradient λ , we clarified in our preceding work that λ decreases from the periodic state through the bifurcation process and reaches a minimum in the chaotic state, based on our preceding work on the SEIR model [29] and the Rössler model [30] throughout a series of period-doubling cascade through chaos. The decrease of the magnitude of λ can be considered to be the result of fluctuations mixed in a deterministic, nonlinear dynamical system [15]. With respect to the

252	fluctuations, two possibilities have been postulated by the author's group [15,30]; first,
253	the amplitude fluctuation could be generated by an instability due to the nonlinearity of
254	the system, as clarified in the result using the Rössler model, or the fluctuations could
255	result from undeterministic noise. In both cases, the magnitude of λ decreases because the
256	high-frequency components do not decline too rapidly [15,33]. In the present study, we
257	confirmed that the magnitude of λ for the pre-Olympics period is smaller than that of the
258	post-Olympics period. This result reflects the relatively high complex variations of the
259	data in the pre-Olympics period, which appears to support Sapkota et al.'s finding that,
260	among Japan's 47 prefectures, the number of prefectures exhibiting chaotic
261	characteristics was lower after the Tokyo Olympics than before [8]. A detailed study
262	investigating chaotic characteristics for each prefecture in Japan is the subject of a
263	forthcoming study.

264

265 **Conclusions**

In general, biological phenomena are both nonstationary and nonlinear, and transit from one state to another in a complicated manner. Based on the results obtained in the present study, the periodic structures of epidemics of infectious diseases, including COVID-19, can be said to change over time. It is not appropriate to deal with the entirety

270	of an overall time series incorporating such states. Thus, for elucidating a temporal
271	evolution of nonlinear phenomena, it is preferable to deal with segments of time series of
272	shorter data length via segment time series analysis, as performed in the present study.
273	Investigation of temporal variational structures of disease epidemics with segment time
274	series analysis can be expected to contribute to long-term and effective COVID-19
275	control programs in Japan.
276	In conclusion, the following three results are confirmed in the present study: First
277	the exponential characteristics of PSDs can be observed for the COVID-19 data of Japan
278	in both pre- and post-Olympics periods, which is peculiar to the nonlinear dynamical
279	process. Second, the magnitude of the gradient of exponential PSD for the pre-Olympics
280	period is smaller than that of the post-Olympics period, because of the relatively high
281	complex variations of the data in the pre-Olympics period caused by a deterministic,
282	nonlinear dynamical system and/or undeterministic noise. Third, changes in the periodic
283	structures of the COVID-19 data were already occurring before the Tokyo Olympic
284	Games began in July 2021 and immediately after the mass and workplace vaccination
285	programs were introduced in April 2021, indicating that the findings of theoretical studies
286	for measles control programs may also apply to the COVID-19 data.

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Jan-20 Mar-20 May-20 Jul-20 Sep-20 Nov-20 Jan-21 Mar-21 May-21 Jul-21 Sep-21 Nov-21 Jan-22 Mar-22 Jun-22 Aug-22 Oct-22 Dec-22

time

