

# Simple model for Covid-19 epidemics – back-casting in China and forecasting in the US

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## **Abstract and Findings**

In our previous work, we analyze, in near-real time, evolution of Covid-19 epidemic in China for the first 22 days of reliable data (up to February 6, 2020). In this work, we used the data for the whole 87 days (up to March 13, 2020) in China and the US data available till March 31 (day 70) for systematic evaluation of the logistic model to predict epidemic growth. We sequentially estimated sets of model parameters (maximum number of cases  $K$ , growth rate  $r$ , and half-time  $t_0$ ) and the epidemic “end time”  $t_{95}$  (defined as the time when the number of cases, predicted or actual, reached 95% of the maximum). The estimates of these parameters were done for sequences of reported cases growing daily (back-casting for China and forecasting for the US). In both countries, the estimates of  $K$  grew very much in time during the exponential and nearly exponential phases making longer term forecasting not reliable. For the US, the current estimate of the maximum number of cases  $K$  is about 265,000 but it is very likely that it will grow in the future. However, running estimates of the “end time”  $t_{95}$  were in a much smaller interval for China (60 – 70 days *vs.* the actual value of 67). For the US, the values estimated from the data sequences going back two weeks from now range from 70 to 80 days. If the behavior of the US epidemic is similar to the previous Chinese development, the **number of reported cases** could reach a **maximum around April 10 to 14**.

## **Introduction**

In our previous recent work (Hermanowicz 2020), we used a simple logistic model to analyze the evolution of data on Covid-19 cases as reported in mainland China by the National Health Commission of the People’s Republic of China (NHC 2020). This initial analysis was done in three phases in near-real time (up to Jan. 30, Feb. 3, and Feb 6). The analysis resulted in a sequence of continually updated forecasts of the epidemic dynamics. Although the predicted maximum numbers of cases increased as new data became available, they systematically underestimated final reported numbers (even without accounting for a major change in reporting criteria in China on February 12 resulting in a large surge of new reported cases). However, the successive **predicted dynamics** of the epidemic were **remarkably close** to the final real-world outcome. We explore this issue further in this work where we use the full reported dataset for mainland China for **systematic back-casting** of the epidemic.

At the same time, when this work is being conducted, in the US we are experiencing a fast developing Covid-19 epidemic that in some aspects is similar to China but with a delay. We use the experience from our analysis of the situation in China to **forecast** further evolution of coronavirus cases in the United States. Obviously, our predictions are based on the data currently available. These predictions do not account for any possible other secondary sources of infection, changes of diagnostics or reporting, or virus mutation.

Modelling the epidemics and infection dynamics is very important and numerous results have been recently reported for worldwide Covid-19 outbreak (Chen, Rui et al. 2020, Chen, Cheng et al. 2020, Hong, He et al. 2020, Hui, Azhar et al. 2020, Imai, Cori et al. 2020, Imai, Dorigatti et al. 2020, Li, Guan et al. 2020, Linton, Kobayashi et al. 2020, Liu, Hu et al. 2020, Liu, Hewings et al. 2020, Roosa, Lee et al. 2020, Shen, Peng et al. 2020, Wu, Leung et al. 2020, Zhang and Wang 2020, Zhao, Lin et al. 2020, Zhou, Hong et al. 2020, Ziff and Ziff 2020). Many reported models are complicated, incorporate tentative assumptions and need parameters estimates that are not reliable as underscored by Fong and coworkers (Fong, Li et al. 2020).

In this work, we present the results of fitting a very simple logistic model to the available data and a forecast of new infections. In contrast to other models, the logistic model does not include any external assumptions and is derived completely from available data.

## Logistic Model and its Application

The logistic model is one of the simplest used in population dynamics and has been used specifically for epidemics for a long time (Bailey 1950, Cockburn 1960, Mansfield and Hensley 1960, Jowett, Browning et al. 1974, Waggoner and Aylor 2000, Koopman 2004, Bangert, Molyneux et al. 2017). In our earlier analysis of the developing epidemic in China, we used a discrete version of the model due to its uncomplicated structure and easy calculations.

In discrete time, more appropriate to daily reported infection cases, the logistic model becomes

$$P(t + 1) = R_0^* P(t) \left[ 1 - \frac{P(t)}{K} \right] \quad (1)$$

where  $P(t)$  and  $P(t+1)$  are populations (cases) on consecutive days,  $R_0^*$  is the growth rate (basic reproduction number in epidemiology) at the beginning of the logistic growth, and  $K$  is the limiting population (maximum cases).

However, expressing the growth of population  $P$  in continuous time  $t$  allows to formulate the model as an ordinary first-order differential equation describing dynamic evolution of the population  $P$  (in our case the number of infected individuals) being controlled by the growth rate  $r$  and maximum cases  $K$  due to limited growth. In continuous time  $t$ , the change of  $P$  is

$$dP/dt = r P \left( 1 - \frac{P}{K} \right) \quad (2)$$

Initially, the growth of  $P$  is close to exponential since the term  $(1 - P/K)$  is almost one. When  $P$  becomes larger (commensurate with  $K$ ) the growth rate slows down with

$$r_e = r \left(1 - \frac{P}{K}\right) \quad (3)$$

becoming an effective instantaneous growth rate.

The solution to Eq. (2) is the well-known sigmoidal function (logistic function)

$$P(t) = \frac{K}{1 + \exp(-r \cdot (t - t_0))} \quad (1)$$

where  $t_0$  is the time when the population reaches one-half of the maximum value  $P(t_0) = \frac{1}{2} K$ . Using a differential version of the model is more convenient since a closed-form solution exists and allows for direct estimation of three model parameters:  $K$ ,  $r$ , and  $t_0$ . The logistic model may be adequate for the analysis of mainland China and the US as a whole since at this time each country can be treated as a unit where a vast majority of cases occurred without any *significant* “import” or “export” of cases.

## Data Analysis

For China, we used data reported daily by the National Health Commission of the People’s Republic of China (NHC 2020) up to March 13, 2020 (day 87 from the outbreak) when only 11 new cases were reported – less than  $2 \cdot 10^{-4}$  of total case number, effectively ending the epidemic on the national level. There is a considerable controversy as to the exact date of the outbreak with most reports pointing to mid-December (Li, Guan et al. 2020, Wang, Horby et al. 2020) while one analysis suggest multiple sources of original infection (Nishiura, Jung et al. 2020). Initially, the outbreak was not recognized and number of *confirmed* cases is not fully known (Wu, Hao et al. 2020). In our analysis, we adopted December 17, 2019 as the best estimate of the outbreak following the work of Zhang and co-workers (Zhang and Wang 2020, Zhang and Wang 2020). In addition, in the initial stages of the epidemic the reported numbers of cases may severely underestimate the actual numbers due to asymptomatic carriers (Zhao, Musa et al. 2020). More accurate numbers can be only estimated after the epidemic (Wu and McGoogan 2020).

The data from China are show in Figure 1 and in the Appendix. As seen in this figure, the cumulative number of cases grew in a sigmoidal fashion. On February 12, 2020 (day 57) the reporting criteria were changed resulting in a one-day increase of about 15,000 cases. We analyzed the subsequent data with this jump and also ignoring it. The logistic model turned out to be quite robust. While the numerical estimates of the maximum number of cases  $K$  was significantly affected by the inclusion or exclusion the jump, the dynamics of the model was much less impacted (see further discussion). In this work, we decided to report the results with the jump as parsing data of new and cumulative cases past day 57 is very unreliable.

In the US, there are numerous agencies tracking the Covid-19 cases at different administrative levels in accordance with multi-tiered structure of the US government. For this reason, we relied on web-based data aggregators (mostly at state level) following daily updates (Covid-19 2020).

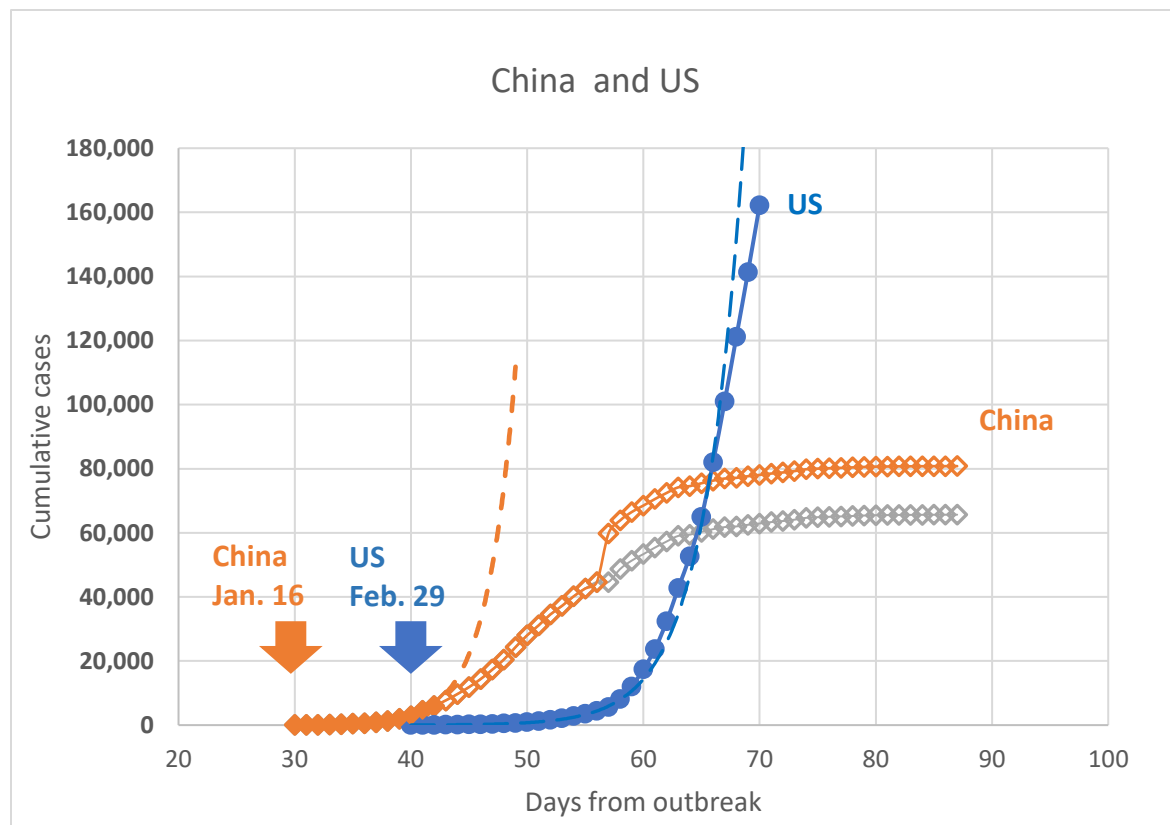


Figure 1 Evolution of reported cases in China and the US.

(Solid points show data used to fit exponential functions – dashed lines)

We used January 21, 2020 as the start of the epidemic in the US (day 1) since on that day the first non-repatriated Covid-19 case was reported. It should be noted that like in China the number of cases in the initial stages is underreported due to the same factors (asymptomatic carriers, initial administrative confusion, limited testing). Despite these problems, the data used in this work are the best currently available. The current evolution of the epidemic in the US is presented in Figure 1 and in the Appendix. Despite smaller population, the number of cases in the US at the time of writing already exceeds that of China. Reasons for such higher numbers are outside the scope of this analysis.

Both, China and the US data are also plotted in the semi-log format (??) to underscore exponential growth of the epidemic in the initial stages – straight line on these plots. In China, exponential growth occurred from day 30 till day 42 as shown in ?? and ?? by the dashed lines. After day 42 (January 28), the number of cases still increased but the rate of growth was

becoming lower and the line representing the cumulative cases deviated from the exponential curve. This feature was also clearly recognized in a previous report (Zhao, Lin et al. 2020).

In the US, exponential growth occurred for a longer period and only very recently (March 27 – 30) **perhaps** starts to deviate from the exponential curve.

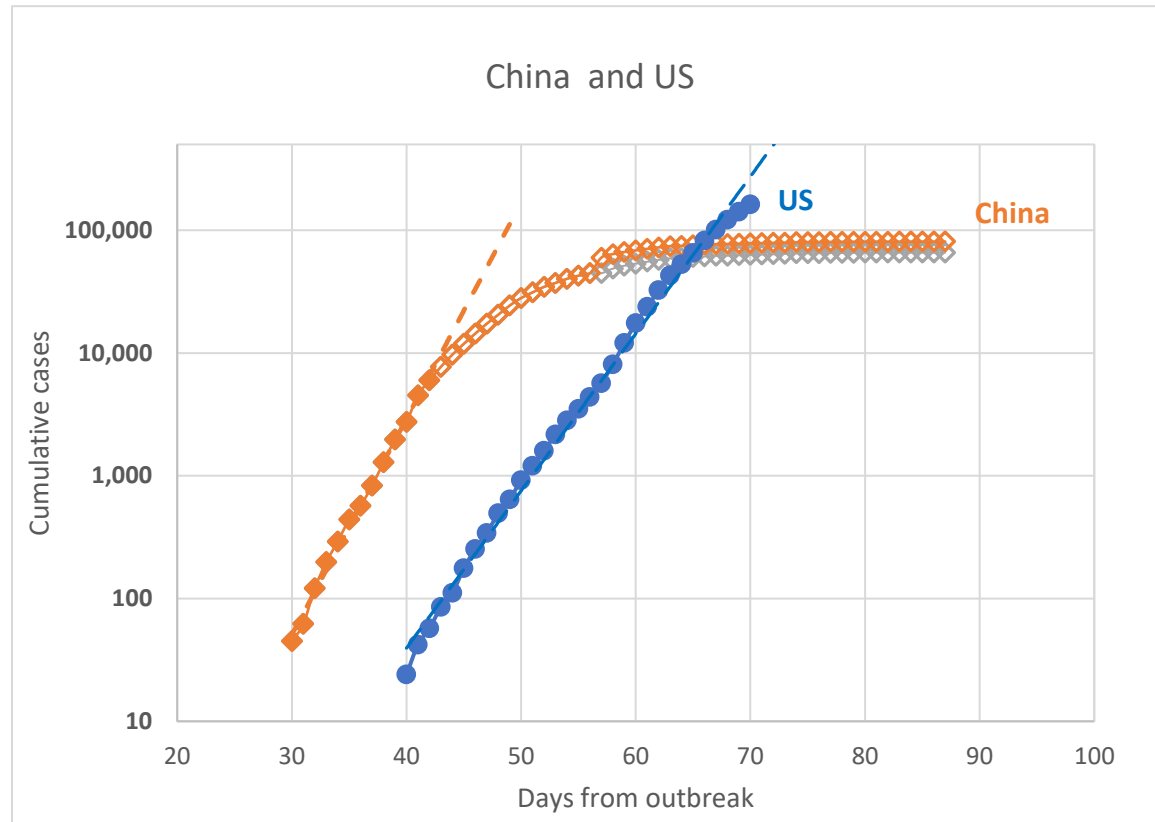


Figure 2 Exponential growth of epidemics (see Figure 1 for notes)

## Model Estimates and Results

For each dataset of reported cumulative case numbers (China and the US), we estimated three parameters of the logistic model (maximum case number  $K$ , growth rate  $r$ , half-time  $t_0$ ) fitting model predictions to the data. We use a custom nonlinear curve fitting procedure employing the Levenberg-Marquardt method for minimization of the residual sum of squares. Similarly to our previous work (Hermanowicz 2020), we estimated model parameters sequentially from datasets growing day after day.

For China, the first dataset contained 5 days from day 38 through 42. The next estimate used 6 days from day 38 through 43. This process was repeated until day 87 when the entire China dataset was used. For the US, the first dataset contained also 5 days from day 43 through 47. The last day of the available sequence for the US was day 70 (March 30, 2020). All resulting estimates are show in the Appendix.

In case of China, where the epidemic growth has essentially ended, the sequential estimation process (back-casting) simulated near-real time analysis of the dynamics. In the US, where we are still in the substantial growth phase, the sequential estimates are indeed performed in near-real time. In addition to three model parameters, for each day we also estimated predicted time for the epidemic to end. For this purpose, we chose arbitrarily time when the predicted number of cases reach 95% of the predicted maximum  $K$ . This time,  $t_{95}$  was calculated from Eq. (4) by setting  $P(t) = 0.95 K$  and is also shown in the Appendix.

### China

Figure 3 shows the development of sequential estimates of the maximum predicted cases  $K$  for China and Figure 4 presents the corresponding “ending times”  $t_{95}$ . As reported earlier (Hermanowicz 2020) for actual near-real time analysis, estimates of predicted maximum cases  $K$  depended very heavily on the length of the dataset used for estimation. As examples, Figure 5 shows a few logistic curves corresponding to selected model parameter estimates on specific days for China. As seen in this figure, the initial estimates (close to the exponential phase) were below 20,000 but they grew to about 100,000 as more data became available and was used for estimate refinement. Obviously, the estimate of  $K$  obtained from the full dataset (up to day 87) matches closely the actual reported number of cases (80,780 vs. 80,807) but it should be noted that the estimates of  $K$  from day 65 (more than 20 days in advance) converged very closely to the actual maximum.

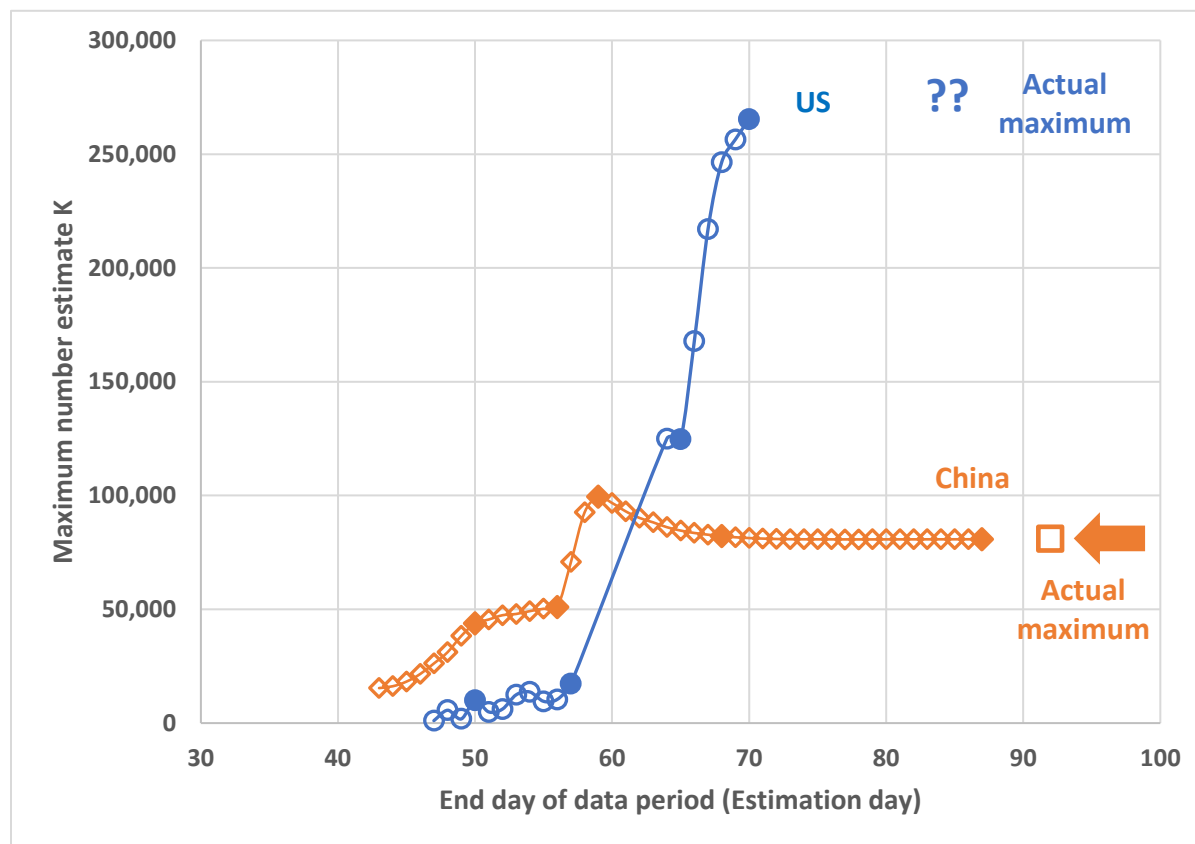


Figure 3 Sequential estimates of  $K$  (solid data points show days for which logistic model predictions are shown in Figure 5 for China and Figure 6 for the US)

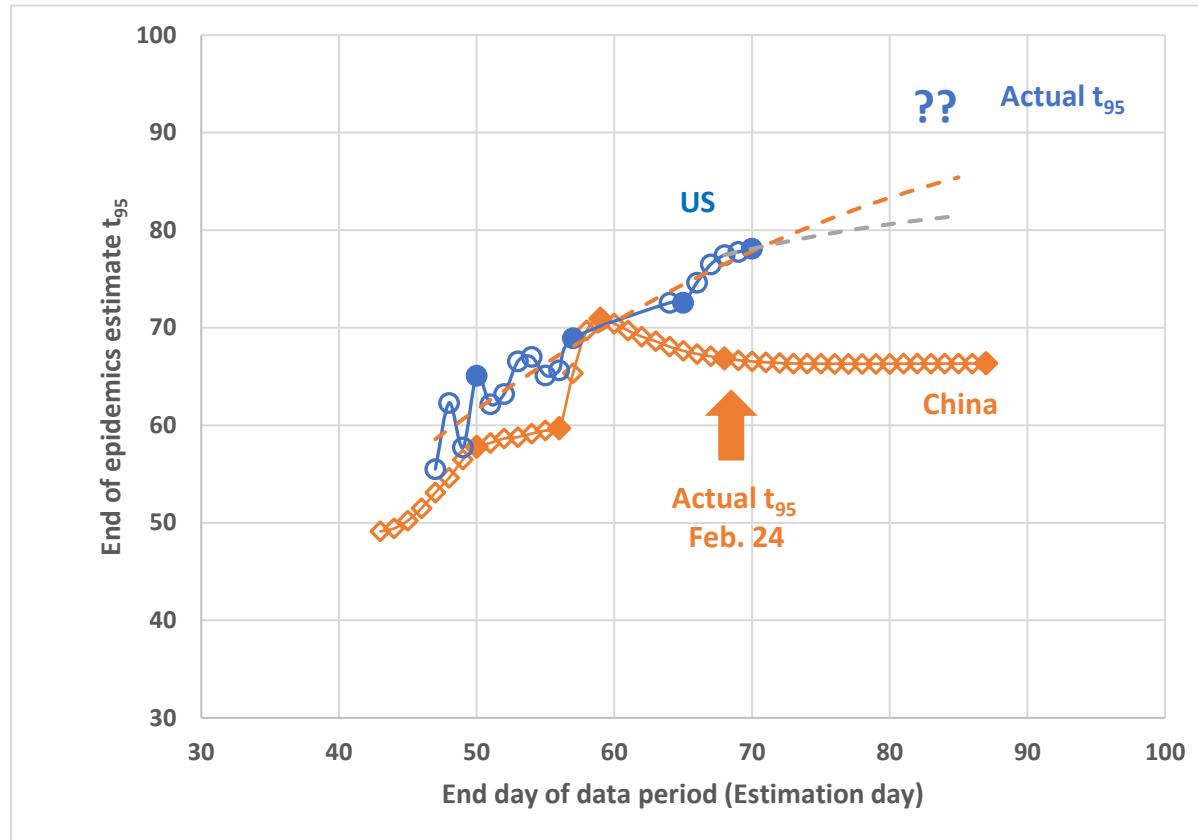


Figure 4 Sequential estimates of "end time"  $t_{95}$  (see notes in Figure 3)

Due to a change in reporting criteria in China on day 57 (February 12), there was a major increase in the number of reported cases that could not be incorporated in the model. As mentioned before, we decided to use all data (with the jump) in any subsequent analysis. The immediate result was a very large increase in the estimated maximum cases  $K$  (Figure 3), approximately doubling it from about 50,000 on day 56 to about 99,400 on day 59. This big increase underscores again the sensitivity of the logistic model to data quality. However, the model is also robust in a longer term as the  $K$  estimates quickly converged toward their ultimate values.

Similarly, there was also a significant jump in the estimates of  $t_{95}$  (see Figure 4) due to the jump in the case numbers. However, it is remarkable that the estimates of the "end time"  $t_{95}$  were much more constrained and much closer to the actual value. Even as early as three weeks before the end of the epidemic the estimates of the "end time" were between 60 and 70 days, very close to the final value of 67 days.

### United States

Unlike China, the epidemic in the US is still at the growth phase, perhaps deviating slightly from the exponential growth. Thus, the available dataset is much smaller and the logistic model estimates are burdened with much larger uncertainty. Currently available estimates of the

maximum cases  $K$  are also shown in Figure 3. They exhibit very large variations increasing from approximately 1,100 on day 47 to approximately 265,000 on day 70 without any sign of leveling off. This large variation is not unexpected since the nearly exponential growth does not contain sufficient information on the actual maximum. In other words, the derivative  $dP/dt$  in Eq. (2) is dominated by the term  $rP$  while  $(1 - P/K) \approx 1$ . This behavior is also seen in the examples of predicted logistic curves for selected sets of estimated parameters  $K, r, t_0$  (Figure 6).

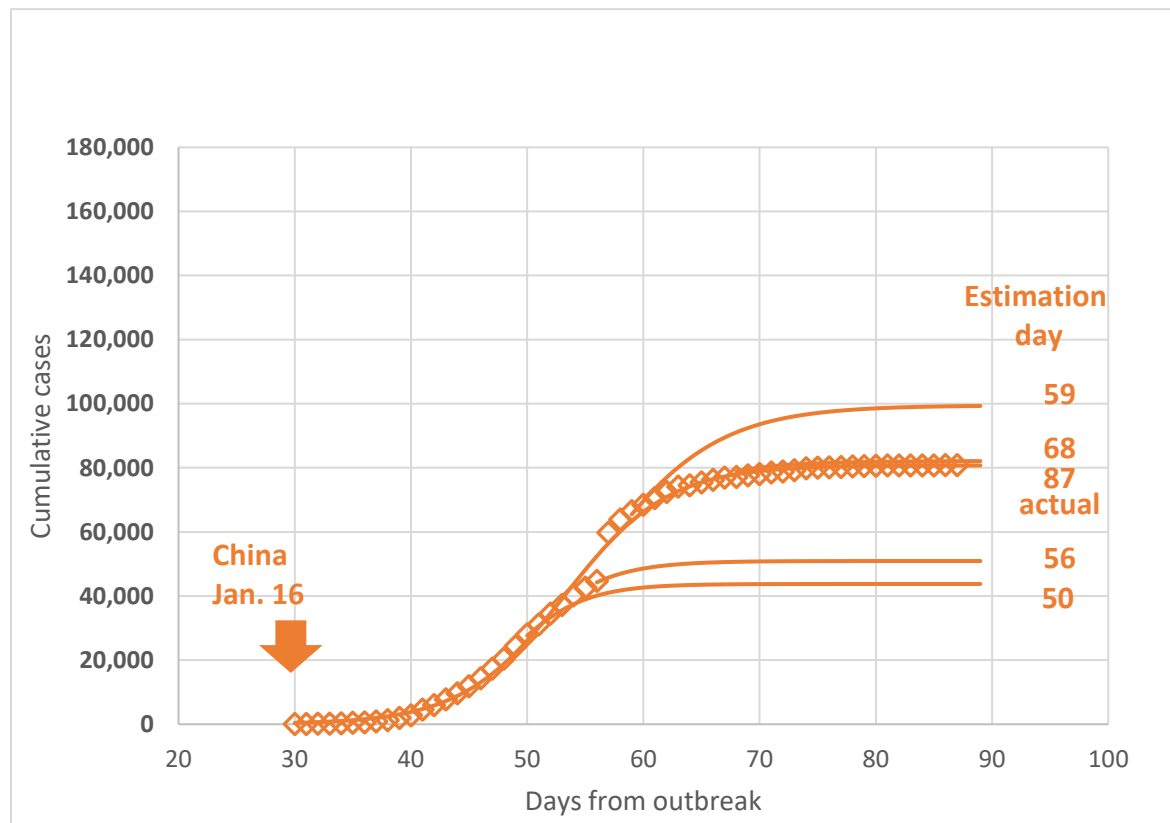


Figure 5 Examples of model predictions for China for selected parameter estimates on specific days

The sequential estimates of the “end time”  $t_{95}$  are plotted in Figure 4. They also tend to increase in time with the increasing number of reported cases but unlike the estimates of  $K$  (and similarly to the Chinese case) it varies in a much smaller interval – 70 to 80 days in the past two weeks. If the behavior of the US epidemic is similar to the Chinese case, we could expect further leveling off of  $t_{95}$  at slightly above 80 days. If this **bold prediction** will hold, we could see the end of the epidemic growth around 80 – 85 days after its origin, around April 10 to 14. Of course, the end here is defined as the cessation of new cases and not the complete recovery of the infected patients.



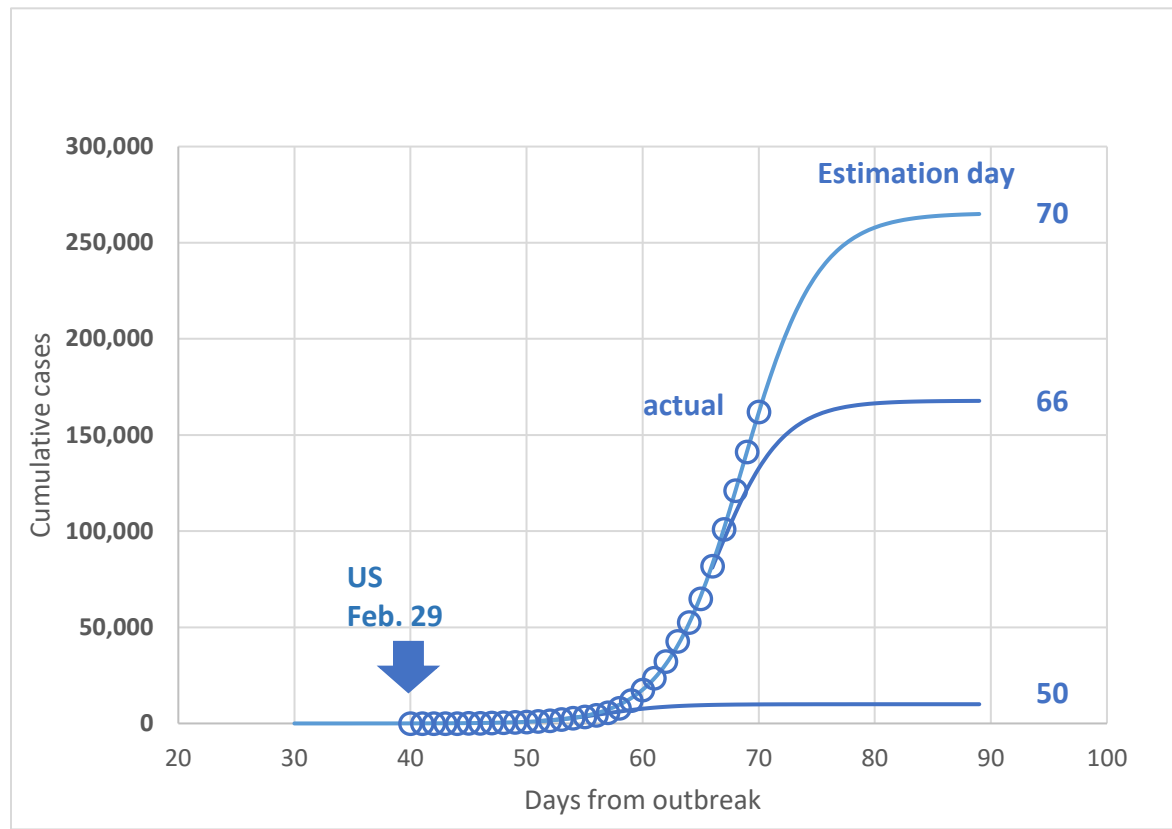


Figure 6 Examples of model predictions for the US for selected parameter estimates on specific days

## Declarations

### *Ethics approval and consent to participate*

The ethical approval or individual consent was not applicable.

### *Availability of data and materials*

All data and materials used in this work were publicly available.

### *Consent for publication*

Not applicable.

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### *Disclaimer*

The funding agencies had no role in the design and conduct of the study; collection, management, analysis, and interpretation of the data; preparation, review, or approval of the manuscript; or decision to submit the manuscript for publication.

### *Conflict of Interests*

The author declared no competing interests.

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## Appendix

*Table A- 1 Number of cases in China*

Date	Day since outbreak	Cumulative Cases
January 16, 2020	30	45
January 17, 2020	31	62
January 18, 2020	32	121
January 19, 2020	33	198
January 20, 2020	34	291
January 21, 2020	35	440
January 22, 2020	36	571
January 23, 2020	37	830
January 24, 2020	38	1,287
January 25, 2020	39	1,975
January 26, 2020	40	2,744
January 27, 2020	41	4,515
January 28, 2020	42	5,974
January 29, 2020	43	7,711
January 30, 2020	44	9,692
January 31, 2020	45	11,860
February 1, 2020	46	14,380
February 2, 2020	47	17,307
February 3, 2020	48	20,467
February 4, 2020	49	24,324
February 5, 2020	50	28,018
February 6, 2020	51	31,161
February 7, 2020	52	34,546
February 8, 2020	53	37,198
February 9, 2020	54	40,171
February 10, 2020	55	42,638
February 11, 2020	56	44,653
February 12, 2020	57	59,804
February 13, 2020	58	63,851
February 14, 2020	59	66,492
February 15, 2020	60	68,500
February 16, 2020	61	70,548
February 17, 2020	62	72,436
February 18, 2020	63	74,185
February 19, 2020	64	74,576
February 20, 2020	65	75,465
February 21, 2020	66	76,288
February 22, 2020	67	76,936
February 23, 2020	68	77,150
February 24, 2020	69	77,658

February 25, 2020	70	78,064
February 26, 2020	71	78,494
February 27, 2020	72	78,824
February 28, 2020	73	79,251
February 29, 2020	74	79,824
March 1, 2020	75	80,026
March 2, 2020	76	80,151
March 3, 2020	77	80,270
March 4, 2020	78	80,404
March 5, 2020	79	80,547
March 6, 2020	80	80,646
March 7, 2020	81	80,690
March 8, 2020	82	80,730
March 9, 2020	83	80,749
March 10, 2020	84	80,773
March 11, 2020	85	80,788
March 12, 2020	86	80,796
March 13, 2020	87	80,807

*Table A- 2 Number of cases in the US*

Date	Day since outbreak	Cumulative Cases
January 21, 2020	1	1
January 24, 2020	4	2
January 25, 2020	5	3
January 26, 2020	6	5
January 30, 2020	10	6
January 31, 2020	11	7
February 1, 2020	12	8
February 2, 2020	13	11
February 5, 2020	16	12
February 20, 2020	31	14
February 26, 2020	37	15
February 28, 2020	39	19
February 29, 2020	40	24
March 1, 2020	41	42
March 2, 2020	42	57
March 3, 2020	43	85
March 4, 2020	44	111
March 5, 2020	45	176
March 6, 2020	46	253
March 7, 2020	47	340
March 8, 2020	48	493
March 9, 2020	49	640
March 10, 2020	50	919
March 11, 2020	51	1,201
March 12, 2020	52	1,598
March 13, 2020	53	2,161
March 14, 2020	54	2,825
March 15, 2020	55	3,497
March 16, 2020	56	4,372
March 17, 2020	57	5,656
March 18, 2020	58	8,074
March 19, 2020	59	12,018
March 20, 2020	60	17,439
March 21, 2020	61	23,710
March 22, 2020	62	32,341
March 23, 2020	63	42,749
March 24, 2020	64	52,685
March 25, 2020	65	64,916
March 26, 2020	66	81,964
March 27, 2020	67	100,997
March 28, 2020	68	121,105



March 29, 2020	69	141,288
March 30, 2020	70	162,161

Table A- 3 Sequential estimates of logistic model for China

End day	Maximum $K$	Rate $r$	Mid-time $t_0$	End time $t_{95}$
42	2.257E+04	0.445	44.3	50.9
43	1.540E+04	0.479	43.0	49.1
44	1.620E+04	0.471	43.2	49.4
45	1.824E+04	0.448	43.7	50.2
46	2.157E+04	0.416	44.4	51.5
47	2.621E+04	0.382	45.4	53.1
48	3.116E+04	0.355	46.3	54.6
49	3.829E+04	0.326	47.5	56.5
50	4.377E+04	0.31	48.3	57.8
51	4.552E+04	0.304	48.5	58.2
52	4.740E+04	0.299	48.8	58.6
53	4.796E+04	0.297	48.9	58.8
54	4.921E+04	0.292	49.1	59.1
55	5.024E+04	0.288	49.2	59.5
56	5.093E+04	0.284	49.3	59.7
57	7.080E+04	0.226	52.3	65.3
58	9.266E+04	0.198	54.9	69.7
59	9.947E+04	0.192	55.6	70.9
60	9.672E+04	0.195	55.3	70.4
61	9.304E+04	0.199	54.9	69.7
62	9.017E+04	0.203	54.6	69.1
63	8.820E+04	0.206	54.3	68.6
64	8.610E+04	0.21	54.0	68.1
65	8.461E+04	0.213	53.8	67.6
66	8.356E+04	0.216	53.7	67.3
67	8.280E+04	0.218	53.6	67.1
68	8.214E+04	0.22	53.5	66.8
69	8.167E+04	0.222	53.4	66.7
70	8.132E+04	0.223	53.4	66.5
71	8.108E+04	0.224	53.3	66.4
72	8.091E+04	0.225	53.3	66.4
73	8.080E+04	0.226	53.3	66.3
74	8.077E+04	0.226	53.3	66.3
75	8.075E+04	0.226	53.3	66.3
76	8.074E+04	0.226	53.3	66.3
77	8.073E+04	0.226	53.3	66.3
78	8.073E+04	0.226	53.3	66.3
79	8.073E+04	0.226	53.3	66.3
80	8.074E+04	0.226	53.3	66.3
81	8.075E+04	0.226	53.3	66.3
82	8.076E+04	0.226	53.3	66.3
83	8.076E+04	0.226	53.3	66.3

84	8.077E+04	0.226	53.3	66.3
85	8.077E+04	0.226	53.3	66.3
86	8.078E+04	0.226	53.3	66.3
87	8.078E+04	0.226	53.3	66.3

Note: Each row contains estimates of the logistic model  $K$ ,  $r$ ,  $t_0$  and the 95% end time  $t_{95}$  estimated from recorded number of cases for the period starting on day 38 and ending on the day in Column 1.

*Table A- 4 Sequential estimates of logistic model for the US*

<b>End day</b>	<b>Maximum <math>K</math></b>	<b>Rate <math>r</math></b>	<b>Mid-time <math>t_0</math></b>	<b>End time <math>t_{95}</math></b>
47	1.074E+03	0.436	48.8	55.5
48	5.659E+03	0.371	54.4	62.3
49	1.851E+03	0.41	50.5	57.7
50	1.000E+04	0.348	56.6	65.1
51	4.923E+03	0.365	54.1	62.1
52	6.144E+03	0.356	54.9	63.2
53	1.243E+04	0.333	57.7	66.6
54	1.368E+04	0.33	58.1	67.0
55	9.575E+03	0.345	56.6	65.1
56	1.042E+04	0.34	57.0	65.6
57	1.729E+04	0.309	59.4	68.9
64	1.250E+05	0.38	64.8	72.6
65	1.248E+05	0.38	64.8	72.5
66	1.678E+05	0.349	66.2	74.6
67	2.170E+05	0.327	67.5	76.5
68	2.465E+05	0.316	68.1	77.5
69	2.565E+05	0.313	68.4	77.8
70	2.654E+05	0.309	68.6	78.1

Note: Each row contains estimates of the logistic model  $K$ ,  $r$ ,  $t_0$  and the 95% end time  $t_{95}$  estimated from recorded number of cases for the period starting on day 43 and ending on the day in Column 1.