

Real-Time Differential Epidemic Analysis and Prediction for COVID-19 Pandemic

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Abstract—In this paper, we propose a new real-time differential virus transmission model, which can give more accurate and robust short-term predictions of COVID-19 transmitted infectious disease with benefits of near-term projection. Different from the existing Susceptible-Exposed-Infected-Removed (SEIR) based virus transmission models, which fits well for pandemic modeling with sufficient historical data, the new model, which is also SEIR based, uses short history data to find the trend of the changing disease dynamics for the infected, the dead and the recovered so that it can naturally accommodate the adaptive real-time changes of disease mitigation, business activity and social behavior of populations. Our work is inspired by the observation that contagious disease transmission prediction is similar to weather prediction: only short term prediction is typically accurate due to many time-varying interplaying factors as well as social and behavior uncertainties involved. On the other hand, accurate short-term prediction such as one week or ten days can give local government and hospital decision makers sufficient lead time for healthcare resources and critical personnel planning to provide in-patient treatment. As the parameters of the improved SEIR models are trained by short history window data for accurate trend prediction, our differential epidemic model, essentially are window-based time-varying SEIR model. Since SEIR model still is a physics-based disease transmission model, its near-term (like one month) projection can still be very instrumental for policy makers to guide their decision for disease mitigation and business activity policy changes in a real-time. This is especially useful if the pandemic lasts more than one year with different phases across the world like 1918 flu pandemic. Numerical results on the recent COVID-19 data from China, Italy and US, California and New York states have been analyzed. Based on the projection as of April 13, 2020 from the proposed model, the time for peak medical resource usage for US as a whole will be around the beginning of May. Also US will reach the peak in terms of daily new infected cases and death cases around middle of April. The total cumulative infected cases will reach to peak of 1.09 million people around June 12, 2020 and the estimated total death cases will reach to 90K in the end.

I. INTRODUCTION

The novel coronavirus (COVID-19) epidemic is generating significant social, economic, and health impacts and has highlighted the importance of real-time analysis and prediction of emerging infectious diseases and health care resource and personnel planning and economical activity guiding.

One of the well-known models that is reasonably predictive for human-to-human transmission is the so-called Susceptible-Infectious-Removed (SIR) model, which was published in its first form around the 1920s [20]. The model later has been extended to consider more complicated situations such as the Susceptible-Exposed-Infected-Removed (SEIR) model [2]. Those models are very successful to describe how the disease dynamics will change over time once more sufficient data are available (from outbreak to finish). Recently those models

have been applied to study recent COVID-19 transmissions in different countries with certain successes [3], [14]–[16], [24]. For example, it is observed that city-wide lockdown can lower the transmission rate substantially from those models. On the other hand, the data-driven and curve-fitting methods for the prediction of COVID-19 such as Gaussian function based fitting method in IHME projection [9], exponential curving fitting in [23], machine-learning based approaches in [8], [22] can fit the data well. However, those methods generally suffer the lack of physical insights of transmission and will not work well when the data does fit their models well (For instance, two waves of infections). For real time prediction, large projection ranges have to be given, which renders the projection less valuable for medical resources and mitigation policy planning.

Furthermore, the worldwide public health crisis like 1918 pandemic, which killed an estimated 50 million people worldwide, including an estimated 675,000 people in the United States, are difficult to model, even to project [1]. H1N1 flu lasted from April 1917 to April 1919 for two years with three major phases across different parts of world. Cities like San Francisco even experienced strong second waves of death increase when the social distance was relaxed too early. Such long-term multi-phase and multi-year transmission dynamic is very difficult to be captured by existing pandemic models. As a result, real-time short-term prediction and near-term trend projection can give each city and county policy maker and resource planners extremely valuable information to guide the disease mitigation and business open/close decision in a real time.

On the other hand, traditional physics-based SIR/SEIR epidemic modeling and its variants suffer several drawbacks especially for real-time disease transmission predictions as it is static model in which many key parameters such as transmission rate and recovery rates are typically fixed values from fitting. However, for countries like US, the local government interventions and mitigation policies such as active surveillance, contact tracing, quarantine, massive testing, school and business closure, shelter in place, social distancing etc. keep changing to respond the local epidemic situations. Also for each state in US has different time lines for implementing different prevention and mitigation measures, which make the static based prediction even more difficult to predict. Further the social behaviors of population, such as bearing face coverage masks are not consistent through different regions and cities as the pandemic progresses, which will affect the transmission rate as well. The availability of healthcare resources of each city and county, which are also changing factors, which

may also affect recovery rate. As a result, existing static SEIR models do not fit well for real-time disease prediction as the key parameters such as transmission rate, recovery rate, which is also closely related to the effective reproduction rate R_0 , are time-varying parameters. On the other hand, one important observation is that *contagious disease transmission prediction is similar to weather prediction: only short term prediction is accurate due to many time-varying interplaying factors as well as social and behavior uncertainties involved*. The widely watched IHME (Institute for Health Metrics and Evaluation) model for real-time COVID-19 epidemic prediction [9] is purely based on mathematic curve fitting techniques, which lacks the theoretical foundation of epidemic transmission found in the SIR models and thus its prediction accuracy is highly debatable.

To mitigate this problem, time-varying SEIR models have been proposed in the past. Dureau *et al* tried to model the time-varying affects of the SEIR models by considering partial and noisy data. They introduced stochastic processes into the SEIR models and solved the resulting stochastic SEIR partial differential equations using Markov Chain Monte Carlo methods in which the transmission is modeled as random walks, which are very expensive to compute [7]. This approach was applied to study the transmission within and outside Wuhan for January to February 2020 [10]. Recently Chen *et al* proposed time-dependent SIR model to model the COVID-19 outbreaks in China [5], In this mode, model parameters are computed in a daily basis. As a result, it lacks the good predictability as all the key parameters have been predicted a prior first, and some ad-hoc methods was introduced to predict the parameters in a near future.

In this work, we propose a new real-time differential virus transmission modeling method, which can give more accurate and robust short-term predictions of COVID-19 transmitted infectious disease while still maintain the near-term projection benefit. The new model is based on enhanced Susceptible-Exposed-Infected-Removed (SEIR) virus transmission model. But it tries to obtain the differential view of pandemic dynamics in a short history window to analyze the short trend of the transmission so that it can be more accurate over different periods of time to accommodate the adaptive changes of disease mitigation, business activity and social behavior of populations. As the parameters of the improved SEIR models are trained by short history window data for accurate trend prediction, our differential epidemic model, essentially are window-based time-varying SEIR model. Since SEIR model still is a physics-based disease transmission model, its near-term (like one month) projection can still be very instrumental for policy makers to guide their decision for disease mitigation and business activity policy changes in a real-time. Numerical results on the recent COVID-19 data from China, Italy and US, California and New York states are analyzed. Based on the projection as of April 13, 2020, Based on the projection as of April 13, 2020, the US is estimated to reach the peak in terms of daily infected cases and death cases around middle of April and the actively infected cases will reach the peak around the beginning of May and total cumulative infected cases will reach to peak around June 12 with 1.09 million

people and the estimated total death cases will reach to 90K in the end.

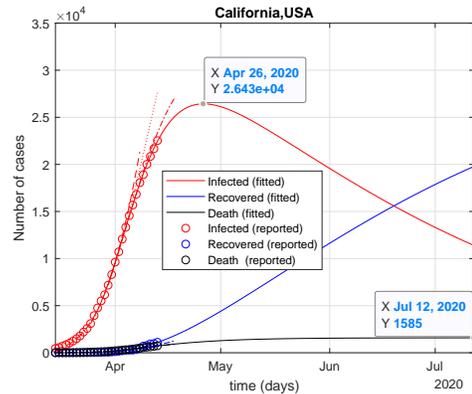


Fig. 1: Modeling and predictions of the proposed differential SEIRDP model for California from early March to later July 2020

Fig. 1 illustrates the modeling and prediction results from the proposed differential SEIR model for the COVID-19 disease for California from early March to later July 2020. As we can see, at the beginning, the infected grows very fast, the projected growth also reflects such fast changing rates. But as social distancing and stay at home policies were introduced across cities and counties in California in the later March, the growth rate went down, the projected growth at different time point also reflects such trends. Based on the projection of our model at April 13, 2020, the infected case will reach to the peak about 26.4K around April 26 in California, which indicates the peak medical resources needed. In contrast, the well-watched IHME’s prediction [9] predicts that the peak medical resource needed is around April 17. We will show more significant differences between our models and IHME’s prediction [9] for New York state later.

II. THE ENHANCED SEIR BASE MODEL

In this section, we first present the extended SIR model, which is a extension of classical SEIR model [6], [11], [12], [17]–[19], [21] as the base model for the proposed differential modeling shown later. The proposed base model, called *SEIRDP model*, is similar to the recently proposed generalized SEIR model for studying the COVID-19 disease in Wuhan and China [16]. We removed the quarantine compartment in the proposed SEIRDP model as there is no quarantine data for most of countries outside China. The resulting SEIRDP (Susceptible, Exposed, Infected, Recovered, Death, Insusceptible (P)) model is shown in Fig. 2. In this base model, we have six states, i.e. $\{S(t), P(t), E(t), I(t), R(t), D(t)\}$, which indicate the number of the susceptible cases, insusceptible cases, exposed cases (infected but not yet be infectious, in a latent period), infectious cases (confirmed with infectious capacity), recovered and immune cases and closed cases (or death). Then the total number of population in a certain region or county is $N = S + P + E + I + R + D$. The coefficients $\{\alpha, \beta, \gamma^{-1}, \lambda^{-1}, \kappa\}$ represent the protection rate, infection rate, average latent time, cure rate, and mortality rate, respectively. The introduction of insusceptible compartment

represents gradual changing (or growing) population, which will not be infected due to some strong disease mitigation measures such as enforced shelter in place, strict city lockdown in China and European countries. The basic reproduction number, R_0 , represents the number of secondary infections from a primary infected individual in a fully susceptible population, which can be computed by [16]

$$R_0 = \beta\lambda^{-1}(1 - \alpha)^n \quad (1)$$

where n is the number of days. We remark that If we force $\alpha = 0$, the proposed SEIRDP model essentially becomes the classical SEIR model (if we put recovered and death cases into one recovery compartment).

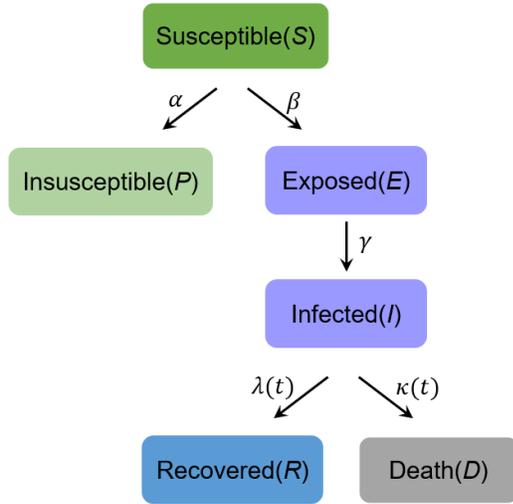


Fig. 2: The proposed enhanced SEIR base model

A. The proposed differential SEIR model

Once we have the base SEIR model, then we can present our differential SEIR model. In this model, basically the key parameters will become time dependent.

In our work, we introduce a time window concept, which represents a short period of time in a few days. For instance five days can be a good time window. In each time window, all the key parameters in the base SEIR models are constant. This reflects the fact that the transmission and recovery conditions for population does not change in a short window time so that we can use a traditional static SEIR model based on the history of data around this window time and we can also predict a short future with sufficient accurate assuming such disease dynamic does not change dramatically, which is also reasonable. Based on this observation, we can present the resulting ordinary differential equations for the proposed differential SEIR model as follows:

$$\begin{aligned} \frac{dS(t)}{dt} &= -\beta(t_i)\frac{S(t)I(t)}{N} - \alpha(t_i)S(t) \\ \frac{dE(t)}{dt} &= \beta(t_i)\frac{S(t)I(t)}{N} - \gamma(t_i)E(t) \\ \frac{dI(t)}{dt} &= \gamma(t_i)E(t) - \lambda(t_i, t)I(t) - \kappa(t_i, t)I(t) \\ \frac{dR(t)}{dt} &= \lambda(t_i, t)I(t) \\ \frac{dD(t)}{dt} &= \kappa(t_i, t)I(t) \\ \frac{dP(t)}{dt} &= \alpha(t_i)S(t) \end{aligned} \quad (2)$$

where time t belongs to the i th time window. If we use t_i to indicate the last day in the window i , then we have $t \in [t_i - w, t_i]$, where w is the window size. The cure rate $\lambda(t_i, t)$ and mortality rate $\kappa(t_i, t)$ are time-dependent, which again are dependent on two parameters. They again are time-window dependent (explained below):

$$\begin{aligned} \lambda(t_i, t) &= \lambda_0(t_i)[1 - \exp(-\lambda_1(t_i)t)] \\ \kappa(t_i, t) &= \kappa_0(t_i)\exp(-\kappa_1(t_i)t) \end{aligned}$$

Those two equations basically say that cure rate or recovery rate $\lambda(t)$ goes up exponentially over a time and the mortality rate $\kappa(t)$ goes down exponentially over time [5].

We notice that all the key parameters for the enhanced SEIR model are time-varying instead of fixed values. But they are so-called *time window dependent*. Specifically, we select $w = 5$ days as a window (the window size is a hyper parameter and can be optimized for different regions and countries). We perform each prediction over each non-overlapping window and then slide one window forward for next prediction. As a result, in i th window, the seven parameters, $\{\alpha(t_i), \beta(t_i), \gamma^{-1}(t_i), \lambda_0^{-1}(t_i), \lambda_1^{-1}(t_i), \kappa_0(t_i), \kappa_1(t_i)\}$ are kept constant. Those parameters will be obtained via a regression process over the given date for $\{I(t), R(t), D(t)\}$ in a given short history. In this paper, we use a nonlinear least-squares solver [4] to estimate the parameters by the expression

$$\hat{\theta} = \arg \min_{\theta} := \left\| \text{SEIRDP}(\theta, \text{time}) - \begin{bmatrix} I \\ R \\ D \end{bmatrix} \right\|^2 \quad (3)$$

where $\theta = \{\alpha(t_i), \beta(t_i), \gamma^{-1}(t_i), \lambda_0^{-1}(t_i), \lambda_1^{-1}(t_i), \kappa_0(t_i), \kappa_1(t_i)\}$, $\hat{\theta}$ is the parameters of estimated model, *time* is the time from the real data, $\{I, R, D\}$ are the infected, recovered and death cases from the real data, and $\text{SEIRDP}(\cdot)$ represents the SEIRDP model. The short history can be $h = 10$ days or $h = 15$ days, which is also another hyper parameter for our model. Since all the parameters are time window dependent, the reduction number becomes time dependent, which is also called *effective reproduction number*, R_t at time t in i th time window becomes

$$R_t(t_i) = \beta(t_i)\lambda^{-1}(t_i) \prod_{j=1}^n (1 - \alpha_j) \quad (4)$$

B. Model parameter estimation for differential SEIR models

For the proposed differential SEIR model, To obtain the seven $\{\alpha(t_i), \beta(t_i), \gamma^{-1}(t_i), \lambda_0^{-1}(t_i), \lambda_1^{-1}(t_i), \kappa_0(t_i), \kappa_1(t_i)\}$ in the i th time window indicated by t_i , which is the last day in the window i , following regression based optimization is carried out based on the initial states computed from previous time window $\{S(t_{i-1}), P(t_{i-1}), E(t_{i-1}), I(t_{i-1}), R(t_{i-1}), D(t_{i-1})\}$. Specifically, we can rewrite the partial differential equation (2) into the following matrix form:

$$\frac{d\mathbf{Y}}{dt} = \mathbf{A} \cdot \mathbf{Y} + \mathbf{F} \quad (5)$$

where

$$\mathbf{Y} = [S(t) \quad E(t) \quad I(t) \quad R(t) \quad D(t) \quad P(t)]^T$$

$$\mathbf{A} = \begin{bmatrix} -\alpha(t_i) & 0 & 0 & 0 & 0 & 0 \\ 0 & -\gamma(t_i) & 0 & 0 & 0 & 0 \\ 0 & \gamma(t_i) & -\lambda(t_i, t) - \kappa(t_i, t) & 0 & 0 & 0 \\ 0 & 0 & \lambda(t_i, t) & 0 & 0 & 0 \\ 0 & 0 & \kappa(t_i, t) & 0 & 0 & 0 \\ \alpha(t_i) & 0 & 0 & 0 & 0 & 0 \end{bmatrix}$$

$$\mathbf{F} = S(t) \cdot I(t) \cdot \begin{bmatrix} -\frac{\beta(t_i)}{N} & \frac{\beta(t_i)}{N} & 0 & 0 & 0 & 0 \end{bmatrix}^T$$

Then we perform the time domain discretization using simple Back Euler or higher order Runge-Kutta method and we end up of number of algebraic equations. Then we can solve for the seven parameters via least square regression using the given data for the past 10 or 15 days and the initial state conditions computed from the previous time window.

III. RESULTS AND DISCUSSION

A. Analysis for public data from Hubei Province, China

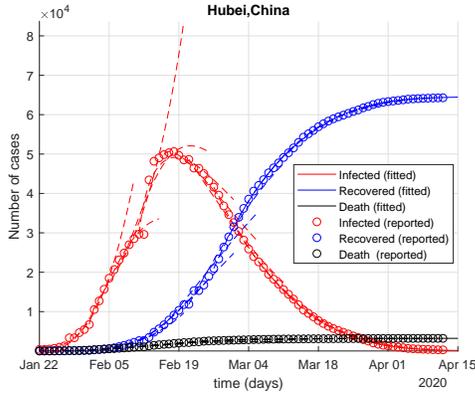


Fig. 3: Predictions of the SEIRDP model for Hubei province, China from January to middle April, 2020

We first show the modeling results for Hubei province of China from early January to the middle of April, 2020. Fig. 3 shows the time evolution of the numbers of the currently infected, the recovered and the death cases over this period. Note that many public websites show the cumulative cases, which are different than the currently infected cases. The currently infected cases equal the cumulative case minus the

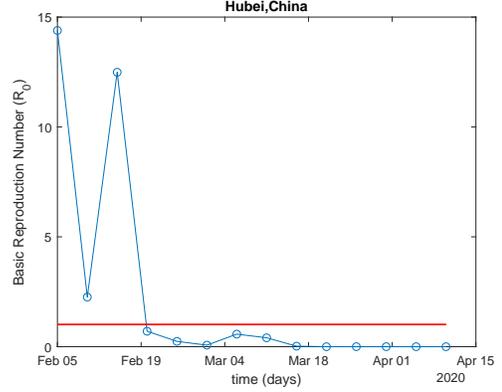


Fig. 4: Effective reproduction number for Hubei province, China from January to middle April, 2020

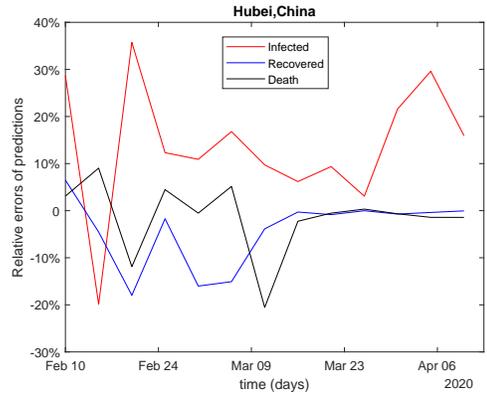


Fig. 5: The relative mean errors of projection for Hubei province China from January to middle of April, 2020

recovered and dead cases. The circles in the figure (in all the figures) are the measured data and the solid line is the last project in early April 2020 as China's pandemic outbreak basically has run its course already and we have all the historical data from early outbreak to finish.

Notice that on Feb. 12, 2020, COVID-19 testing criteria was relaxed in Hubei Province. As a result, there is a huge jump of confirmed infected cases, which can be viewed as an outlier for the date. As a result, the projection based on the history before and around Feb. 12 is quite off the track of actual cases as shown in Fig. 3. But for the most of days over the two month period, the projected and actual measured cases match very well.

Fig. 4 shows the effective reproduction number, R_t , over the same period time. As we can see, R_t becomes less than 1 around Feb. 19, which is about 3 weeks after city lockdown in Wuhan on Feb 23, 2020. This indeed shows the effects of strict city lockdown in Hubei province to reduce the transmission effect of the virus. Feb. 19 is also close to the time when the peak of infected people was reached as shown in Fig. 3. As a result, analysis and prediction of effective reproduction number can give us more insights into how the pandemic dynamics will play out and when the peak or turning points will happen in the real time. Fig. 5 shows the 5-day predicted

mean errors in percentage against the measured data. The mean errors are computed for the average estimated errors in each time window (every five days) between the 5-day projected infected cases and measured cases. This is case for all the mean error computations in the sequel.

B. Analysis and prediction for Italy

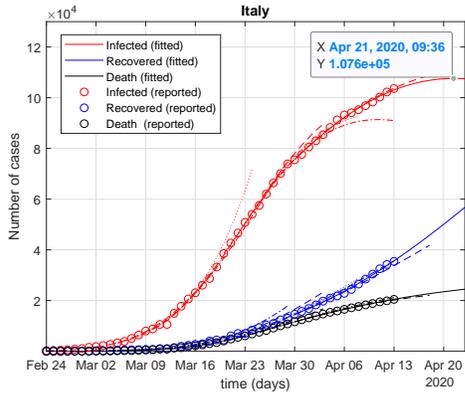


Fig. 6: Predictions of the differential SEIRD model for Italy from later February to middle April, 2020

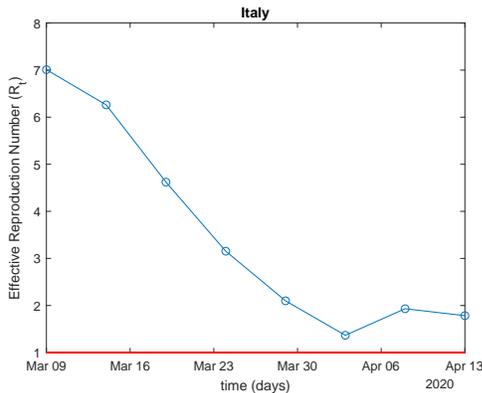


Fig. 7: Effective reproduction number for Italy from later February to middle April, 2020

Fig. 6 shows COVID-19 disease modeling and prediction for Italy from late February to middle of April 2020 as Italy was mostly severely impacted by COVID-19 in Europe. As we can see, our differential models match well for the historical data. The prediction around early March is quite aggressive as the actual growth rate for both infected and death are very high. This is also reflected in the effective reproduction number, which is about 6-7, at those days as shown in Fig. 7. As of April 13, R_t has reached to around 2 and is still going downward. Based on our 10 day prediction, the currently infected cases will reach to the peak around April 21 with about 107K cases. Fig. 8 shows the 5-day projected mean errors. As we can see, as time progresses, the projected error goes down and is limited to about 10% for the three types of cases analyzed.

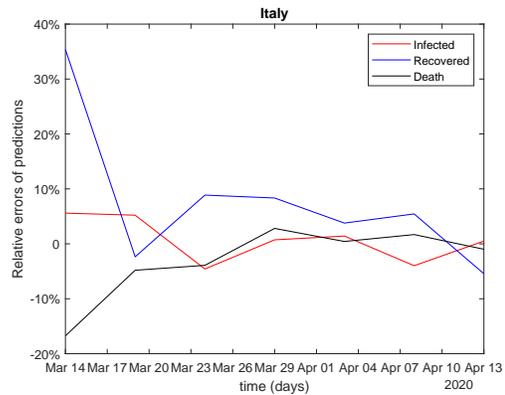


Fig. 8: The relative mean errors of projection for Italy from February to April, 2020

C. Analysis and prediction for United State

For US data, we show the results for US, New York state and California state as New York is the epicenter of the COVID-19 in US. California has the largest population in US. The two states also have dramatically different transmission situations.

Fig. 9 shows first modeling and projection for US from late early March to middle July 2020 for the currently infected, recovery and death cases. The results from the models match the given data very well. Based on the last differential SEIRD model, we project that the infected cases in US will reach to the peak at May 5th, 2020 with about 767K cases, which is also the peak time for medical resources. As comparison, the IHME's projection [9] predicts the peak medical usage is around April 10, 2020.

The effective reproduction numbers over the same time period and the relative projection errors are shown in Fig. 10 and Fig. 11 respectively. As we can see, the effective reproduction number seems higher than basic reproduction number, R_0 , which was estimated about 2-7 for COVID-19 [13]. This may reflect the significant portion of unconfirmed and asymptomatic population at the beginning of this outbreak in US (this is the cases for all the other countries). But as time progresses, R_t tends to level down to a more reasonable range as more confirmed cases have been reported.

Fig. 12 and Fig. 13 show that daily newly confirmed infected cases and daily death cases for US over the same period respectively. The blue lines are the actual data and the brown lines are projected data from April 13 to middle of July 2020. As we can see that the daily infected cases seem reaching the peak around April 10 with about 35K per day and then start to de-escalate. If current trend is held, the infected case will go to almost zero around middle of June, which indicates the end of this COVID-19 pandemic. From Fig. 13, we can see that the daily death reached the peak around April 10 and then go downward gradually. If this trend is held, the daily death will continue well beyond July before it stops and the estimated total death cases will reach about 90K in the end. We want to express that such projection is subject to change due to many changing factors such as mitigation policies and people behaviors in the near term.

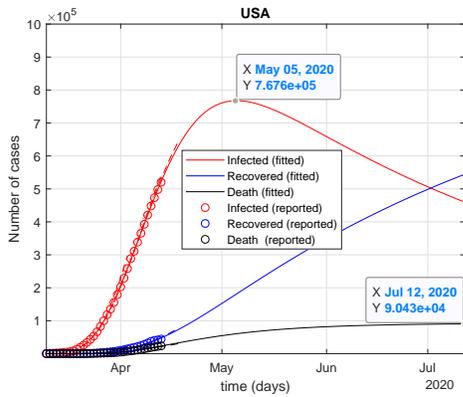


Fig. 9: Predictions of the differential SEIRDP model for US from early March to middle July, 2020

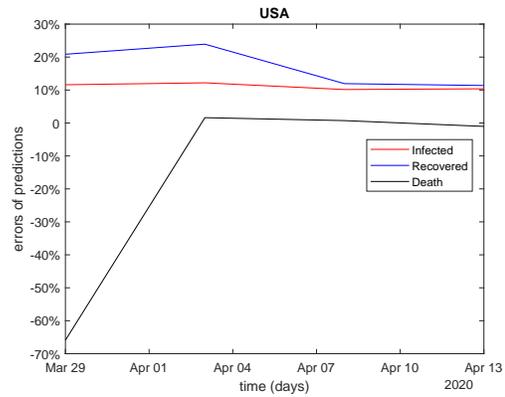


Fig. 11: The relative mean errors of projection for US from early March to middle April, 2020

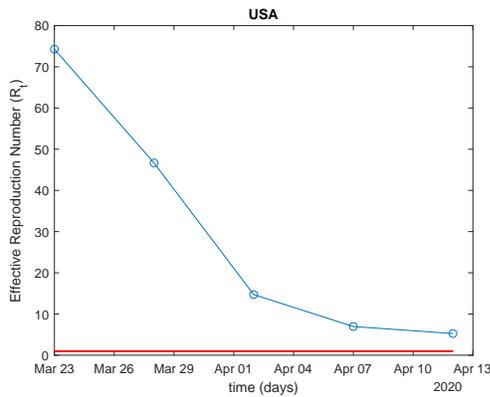


Fig. 10: Effective reproduction number for US from early March to middle April, 2020

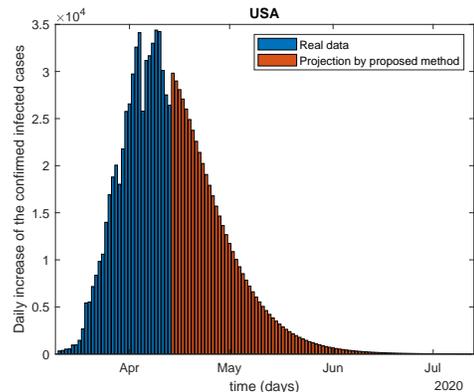


Fig. 12: The daily increase of infected cases measured and projected for US from early March to middle July, 2020

Fig. 14 show the existing daily confirmed infected cases for US over March to middle July. We project it will reach total number probably will reach to about 1.1 millions in June 12.

D. Analysis and prediction for California state

For California, the modeling and projection results from the same period of US are shown in Fig. 9, Fig. 15 and Fig. 16. As we can see from Fig. 9, the currently infected cases will reach the peak (about 26.4K) around April 26. In contrast, IHME's projection [9] predicts that the time for peak medical resource usage is around April 17. The effective reproduction number is around 5 as of April 13, which is close to the observed basic reproduction number for COVID-19, estimated about 2-7 for COVID-19 [13].

Fig. 17, Fig. 18 and 19 show the daily confirmed infected cases, the death cases and the total accumulative infected cases for California over mentioned period respectively. California also reached the peak on April 8 (about 14K) for daily infected and on April 10 for death cases (about 54). But the total infected total is projected to reach 32.7K at May 23, and the estimated total death cases will reach to about 1585 in the end.

E. Analysis and prediction for New York state

For New York State, the modeling and projection results from the same period of US are shown in Fig. 20, Fig. 21 and

Fig. 22. For New York state, the projected currently infected cases will reach to the peak around the beginning of May, which is close to the peak estimation of US. This is no surprise, as half of the infected cases come from New York state from US. In contrast, IHME's projection shows the time for peak medical resource usage is April 8, which indicates significant difference from our model. The estimated effective reproduction numbers from the differential models are reduced to the be less than 5 and continue going downward around April 13, 2020.

Fig. 23, Fig. 24 and Fig. 25 show the daily confirmed infected cases, the death cases and the total accumulative infected cases for New York state over mentioned period respectively. New York state reached the peak around April 10 for both the daily infected increase (about 12K per day). But for daily death cases, it will reach the peak of 932 per day around April 22. But the total infected cases is projected to reach peak of 311.6K on June 15, and the estimated total death cases will reach to about 54.5K in the end.

IV. CONCLUSION

In this paper, we have proposed a new real-time differential virus transmission model, which can give more accurate and robust short-term predictions of COVID-19 transmitted infec-

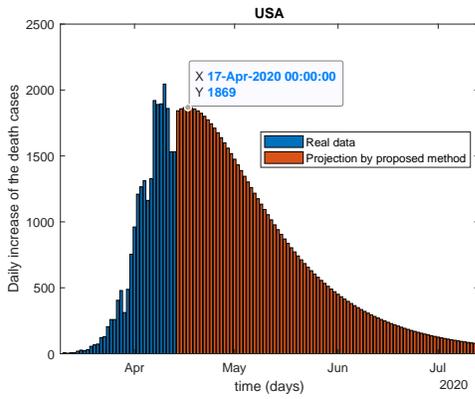


Fig. 13: The daily increase of death cases measured and projected for US from early March to middle July, 2020

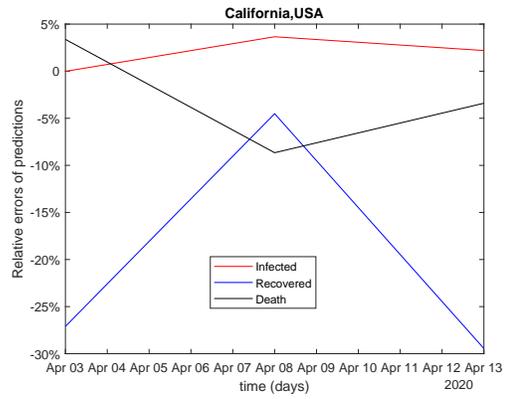


Fig. 16: The relative mean errors of projection for California from early March to middle April, 2020

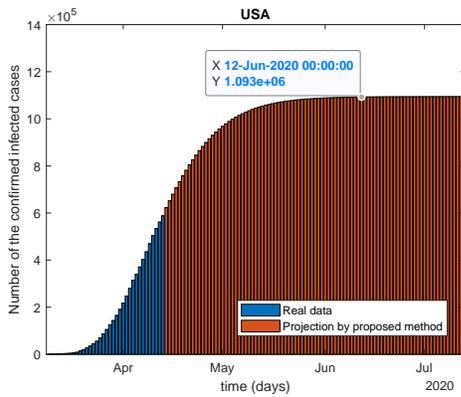


Fig. 14: The number of the confirmed cases measured and projected for US from early March to middle July, 2020

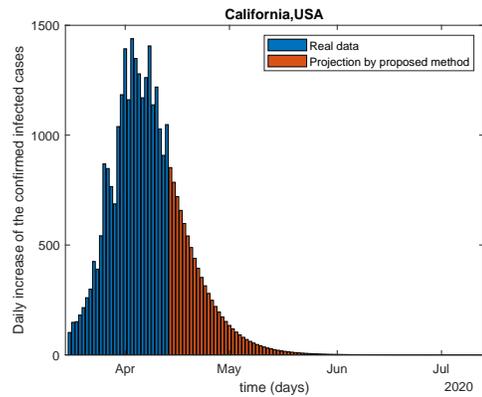


Fig. 17: The daily increase of infected cases measured and projected for California from early March to middle July, 2020

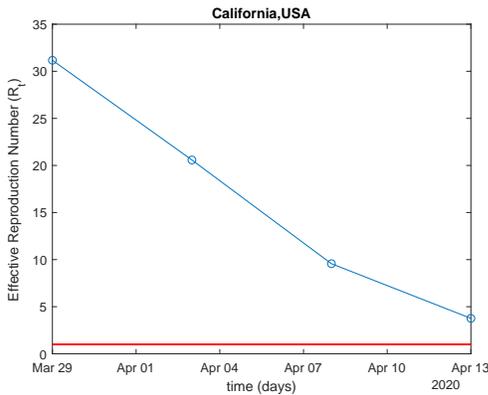


Fig. 15: The estimated effective reproduction number for California from early March to middle April, 2020

tious disease with benefits for near-term projection. The new model is based on enhanced Susceptible-Exposed-Infected-Removed (SEIR) virus transmission model. As the parameters of the improved SEIR models are trained by short history window data for accurate trend prediction, our differential epidemic model, essentially are window-based time-varying SEIR model. Numerical results on the recent COVID-19 data

from China, Italy and US, California and New York states have been analyzed. Based on the projection as of April 13, 2020, the US will reach the peak in terms of daily infected cases and death cases around middle of April and the actively infected cases will reach the peak around the beginning of May, which is also the peak medical resource usage time. The total cumulative infected cases will reach to peak around June 12, 2020 with 1.09 million people and the estimated total death cases will reach to 90K in the end.

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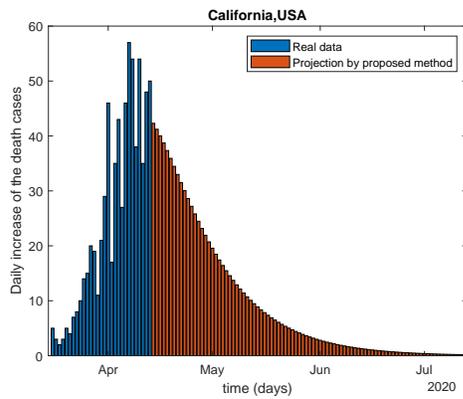


Fig. 18: The daily increase of death cases measured and projected for California from early March to middle July, 2020

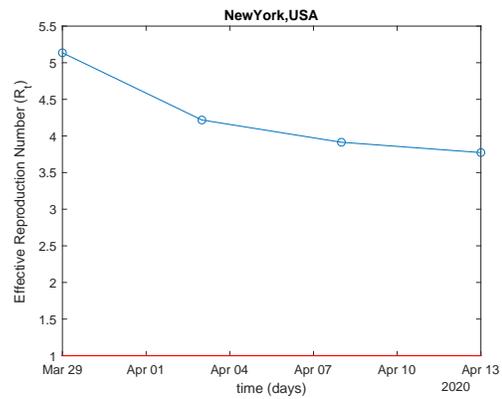


Fig. 21: Effective reproduction number for New York state from early March to middle April, 2020

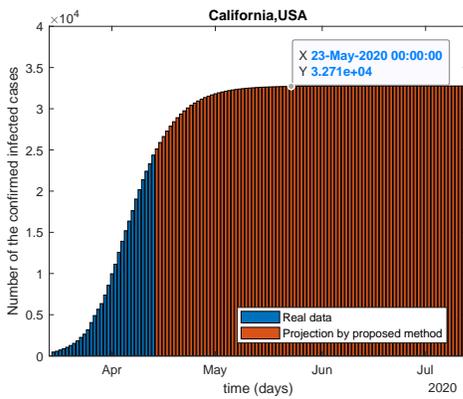


Fig. 19: The number of the confirmed cases measured and projected for California from early March to middle July, 2020

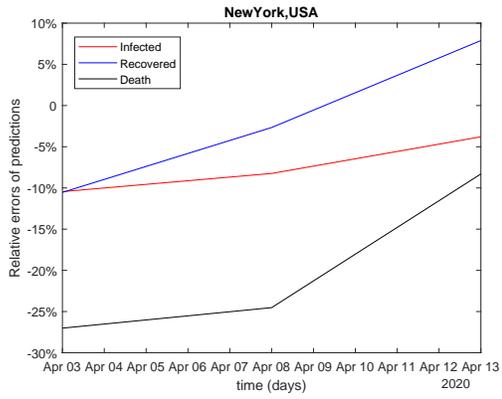


Fig. 22: The relative mean errors of projection for New York state from early March to middle April, 2020

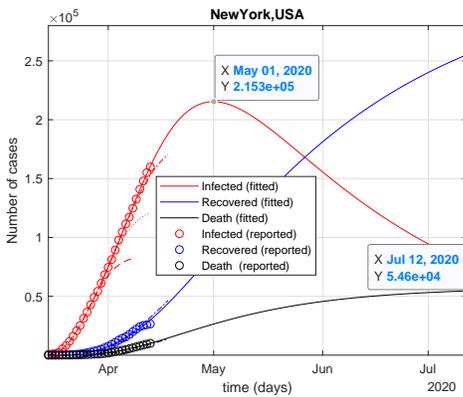


Fig. 20: Predictions of the differential SEIRDP model for New York state from early March to middle July, 2020

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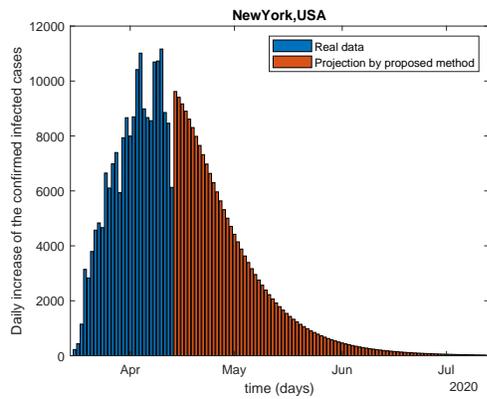


Fig. 23: The daily increase of infected cases measured and projected for NewYork from early March to middle July, 2020

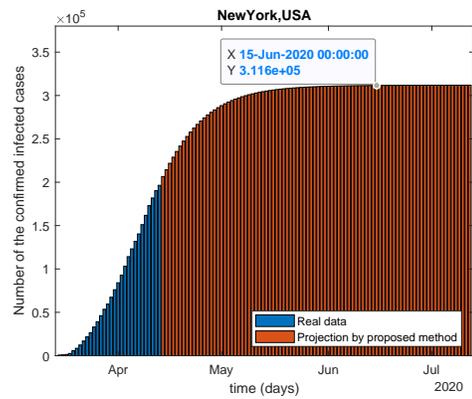


Fig. 25: The number of the confirmed cases measured and projected for NewYork from early March to middle July, 2020

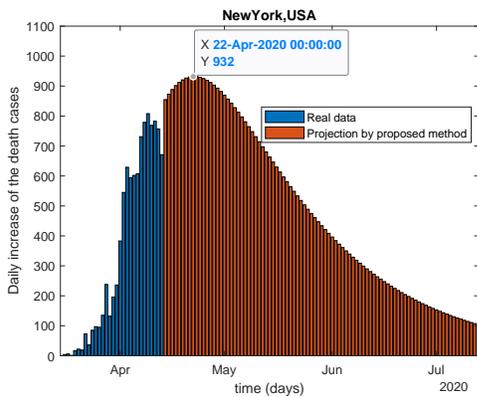


Fig. 24: The daily increase of death cases measured and projected for NewYork from early March to middle July, 2020

number of the wuhan novel coronavirus 2019-ncov,” *Journal of Evidence-Based Medicine*, vol. 13, no. 1, pp. 3–7, 2020. [Online]. Available: <https://onlinelibrary.wiley.com/doi/abs/10.1111/jebm.12376>

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